

Understanding Migration Responses to Local Shocks*

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Abstract

We examine how to interpret estimates from a commonly used migration regression relating changes in local population to exogenous local labor demand shocks. Using a simple model of local labor markets with mobility costs, we find that common conclusions drawn from migration regression estimates are likely to be substantially misleading. Intuitively, the conventional migration regression is misspecified due to the bilateral nature of location choices. Workers choose where to live based not only on the shock to their current location, but also on the shocks to potential alternative locations, which are omitted from the regression. Analytical results and simulations based on Brazilian data show that conventional migration regression estimates are inaccurate for the within-sample effects of observed shocks on local populations and uninformative on the effects of counterfactual shocks to local labor demand. These problems are particularly acute when workers face industry switching costs in addition to geographic mobility costs.

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1 Introduction

Workers’ interregional migration responses are critical in determining the impacts of local economic shocks. The welfare effects of a given shock depend upon whether workers can smooth adverse labor market outcomes by migrating (Yagan, 2014). The speed of migration adjustment affects how long the impacts of local shocks persist (Topel, 1986; Blanchard and Katz, 1992), and a lack of migration response may help explain long-lasting economic effects of changes in local labor demand (Dix-Carneiro and Kovak, 2017, 2019; Autor et al., 2021). Mobility responses determine how local shocks influence inter-regional inequality (Topalova, 2010; Cadena and Kovak, 2016), and differences in mobility responses across demographic groups can drive between-group inequality as well (Bound and Holzer, 2000; Wozniak, 2010; Dix-Carneiro and Kovak, 2015). If migration frictions are particularly large, policy makers may consider programs to help workers relocate.¹

A voluminous literature spanning subfields of economics studies migration responses to local shocks using what we refer to as the “conventional migration regression.” This regression relates local population growth to observed labor demand shocks, as in the following regression specification:

$$\hat{L}_\ell = \beta_0 + \beta \hat{z}_\ell + \varepsilon_\ell, \tag{1}$$

where \hat{L}_ℓ is the proportional change in population in location ℓ , \hat{z}_ℓ is an observed local labor demand shock, and ε_ℓ is the error term. In many cases, researchers find substantial effects of the shocks on local economic outcomes such as wages and employment, but find estimates of β that are small and statistically indistinguishable from zero.² These results have often been used to infer that migration costs are high, that workers are generally unresponsive to changing local economic conditions, or that interregional migration can be ignored in quantitative models.

In this paper, we show that most common interpretations of β in (1) yield misleading conclu-

¹For example, the U.S. Trade Adjustment Assistance program includes funding for distant job search activities and an allowance for relocation costs (Hyman, 2018).

²Examples of papers finding substantial effects of local labor demand shocks on local economic outcomes but with estimates of β that are small and/or statistically indistinguishable from zero include Bound and Holzer (2000) (for those with a high-school degree or less); Topalova (2010); Autor et al. (2013); Dauth et al. (2014); Mian and Sufi (2014); Cadena and Kovak (2016); Dix-Carneiro and Kovak (2017); Dix-Carneiro and Kovak (2019); Yagan (2019); Autor et al. (2021) (except for those age 25-39); Choi et al. (2021); and Faber et al. (2021) (for Chinese import competition), among others. Additional papers estimating a version of (1) and finding substantial or ambiguous population results include Black et al. (2005); Wozniak (2010); McCaig (2011); Bustos et al. (2016); Hakobyan and McLaren (2016); Bartik et al. (2019); Foote et al. (2019); Greenland et al. (2019); Monràs (2020); Albert and Monràs (2020); Notowidigdo (2020); and Albert et al. (2021a), among others.

sions. In particular, the estimate of β can be close to zero even when the observed shock led to substantial spatial reallocation, workers are highly responsive to local conditions, and responses to counterfactual shocks would be large. These problems arise even when the observed shock is “exogenous,” in the sense of being as good as random with respect to unobserved local labor demand and supply shocks.³

The core intuition emerging from our analysis is that the conventional migration regression is misspecified due to the bilateral nature of location choices. When workers consider economic conditions in deciding whether and where to move, their decisions depend upon both the shock to their current location and the shocks facing potential alternative locations. Since workers face different migration costs across origin-destination pairs, the most important potential alternatives differ across initial locations. By omitting the shocks facing these relevant alternative locations, the conventional migration regression in (1) is misspecified, which can lead to poor predictions for the effects of observed shocks on population growth in each location. Moreover, when the omitted shocks to relevant alternative locations are correlated with the shock to the current location, the conventional migration regression suffers from omitted-variable bias. For example, even if workers are very responsive to differences in labor demand conditions, there will be little incentive to migrate when workers’ current and potential alternative locations face very similar labor demand shocks. In this case, the conventional migration regression estimate β will be close to zero even though the true migration elasticity is high.

We analyze these interpretation problems in the context of a static model of local labor markets in which workers face mobility costs and have idiosyncratic preferences for living in different locations. The model is deliberately simple, focusing on costly migration while omitting features such as housing or capital markets. The simplicity of the model allows us to derive an intuitive approximation for the effect of a given vector of local labor demand shocks on local population growth, capturing the intuition just described. The effect of all shocks on a location’s population depends on the direct shock to the location minus the migration-weighted average shock to other locations, which is a summary statistic of relevant spillovers.

We use this model to derive a novel decomposition for β in the conventional migration regression. We show that β increases in i) the ratio of migration and labor demand elasticities, ii) the baseline

³Equation (20) defines “as good as random” in this context.

share of migrants in the national population, and iii) an “attenuation factor” that is below one when shocks are particularly positively correlated between regions with large migration flows. This decomposition allows us to contrast various common interpretations of β against true model-based responses to observed or counterfactual shocks. Examples include interpreting β as the effect of a unit shock to a single location or $\beta(\hat{z}_k - \hat{z}_\ell)$ as the difference in the effects of all shocks on locations k and ℓ . We show that these and similar interpretations provide poor predictions for the true effects on local populations, particularly when the shocks used to estimate β are correlated across migrant-connected locations and thus attenuation is severe.⁴

An extension of the model shows that these interpretation problems are exacerbated when workers face mobility costs across both regions and industries. Many papers estimating (1) analyze local labor demand shocks with a shift-share structure in which typically $\hat{z}_\ell = \sum_n \frac{L_{\ell n}^0}{L_\ell^0} \hat{x}_n$, where \hat{x}_n is a labor demand shock facing industry n , and $L_{\ell n}^0/L_\ell^0$ is industry n ’s initial share of employment in location ℓ . If industry switching costs are large, workers see minimal benefit to moving across locations because they primarily face the shock to their industry no matter where they choose to live. When labor demand shocks have an industry component, the presence of industry switching frictions thus reduces migration beyond what one would observe in a setting with regional frictions alone.⁵

Given the failure of the conventional migration regression to provide accurate predictions of the effects of observed or counterfactual local labor demand shocks, we propose an alternative approach leveraging the model-based expression relating the vector of local shocks to population changes in each location. Given observed labor demand shocks and data on the baseline migration flows between locations (or industry-location pairs in the extended model), one can use nonlinear least squares (NLLS) to estimate the relevant parameter and predict the effects of observed or counterfactual labor demand shocks. While this procedure is specific to our model, the same

⁴We show that β is correctly interpreted as the *average* difference in the effect of *all* shocks across locations facing higher vs. lower direct shocks. While correct, this interpretation is quite limited. Even when β is small, the shocks may have led to substantial spatial reallocation because of variation in migrant-connected locations across places facing similar direct shocks. We also show that, with some caveats, finding $\beta \approx 0$ does approximately imply a lack of confounding from migration when studying the effects of local shocks on local *wage* changes.

⁵Of the papers estimating conventional migration regressions listed in footnote 2, the following use shift-share labor demand shock measures: Topalova (2010); Wozniak (2010); McCaig (2011); Autor et al. (2013); Dauth et al. (2014); Cadena and Kovak (2016); Hakobyan and McLaren (2016); Dix-Carneiro and Kovak (2017); Dix-Carneiro and Kovak (2019); Greenland et al. (2019); Albert and Monràs (2020); Notowidigdo (2020); Autor et al. (2021); Choi et al. (2021); and Faber et al. (2021).

approach can be applied to extended models that include additional economic forces.

To assess the quantitative importance of our insights, we study the effects of simulated shocks in the context of real-world geography and migration patterns. We base our simulations on longitudinal administrative data covering formally employed workers in Brazil, which allow us to observe worker transitions across locations and industries. Due to data limitations, we use formal employment as a proxy for local population in this exercise. We simulate labor demand shocks following a variety of different data-generating processes and generate model-implied local population changes when workers face migration frictions alone or when facing both migration and industry frictions. The resulting population changes are then used to estimate the conventional migration regression, the results of which we compare to the true model-based effects of the simulated labor demand shocks.

The results of this simulation exercise confirm the practical importance of the concerns raised by the theoretical analysis. The regression-based estimates poorly predict the effects of the simulated shocks themselves, and counterfactual estimates are even less accurate, particularly when the observed shock used to estimate β and the counterfactual shocks have very different average correlations between migrant-connected locations. These problems are largest when analyzing industry-level shocks via shift share regressions in the presence of location and industry frictions.

To assess the performance of our model-consistent NLLS procedure we introduce random variation from unobservable factors into the simulation procedure and vary the magnitude of this residual variation.⁶ For all magnitudes of the unobserved component, the predictive performance of this NLLS procedure far outperforms that of the conventional migration regression, which often performs as poorly as an uninformative prediction of zero migration response. The model-based procedure has the best predictive power when estimated using baseline worker flows at the location-industry level, and this relative performance improvement is largest for industry shocks rather than regional shocks. These findings highlight the importance of accounting for observed connections between locations and industries and the value of leveraging data at the location-industry level.

Our results inform the many papers estimating the conventional migration regression in (1), which span development, international, labor, resource, and urban economics.⁷ We emphasize interpretation challenges resulting from cross-location spillovers that violate the stable unit treatment

⁶We do not implement the NLLS procedure in the simulations without additional residual variation because it would fit perfectly by definition.

⁷See footnote 2 for references.

value assumption (SUTVA). A small number of papers in this literature anticipated this spillover issue and introduced ad-hoc controls in an effort to address it. While studying the effects of Chinese import competition on U.S. local population changes, Greenland et al. (2019) control for the weighted average of shocks to other locations, with weights proportional to the squared inverse distance. In studying the effects of droughts on regional labor and capital reallocation in Brazil, Albert et al. (2021b) include a migration-weighted average of drought measures in other locations. Our analysis refines and provides a theoretical rationalization for these approaches to dealing with cross-location spillovers.

Our simple model of costly migration follows the tradition of static gravity models of location choice used to analyze both migration and commuting (e.g. Ahlfeldt et al. (2015); Morten and Oliveira (2018); Monte et al. (2018); Amior and Manning (2019)). The common feature of these models is logistic demand across destinations for each origin, with a network pattern generated by bilateral moving or commuting costs; most closely related in the migration context are the formulations by Tombe and Zhu (2019) and Fan (2019). On the labor demand side, the standard multi-sector Armington model that we employ has been used by Anderson and van Wincoop (2003), Head and Mayer (2014), and Adão et al. (2019), among many others.

Methodologically, our paper is related to Adão et al. (2021), who study how trade linkages generate interregional spillovers in the employment and wage effects of increased Chinese imports in the U.S. Like them, we provide a model-consistent reduced-form equation for the effects of a local labor demand shock in presence of spatial spillovers; our analysis focuses on spillovers from migration while theirs focuses on interregional trade.⁸ Yet, the papers' objectives are quite distinct, with Adão et al. (2021) seeking to estimate aggregate general equilibrium effects of a spatially heterogeneous shock to labor demand and our analysis informing a commonly used reduced-form approach that generally ignores potential spillovers.

The paper proceeds as follows. Section 2 describes the baseline model of local labor markets in which workers face costs of moving across locations, solves the model, and relates model-based expressions to observable quantities. Section 3 defines and characterizes the conventional migration regression coefficient and discusses problems when using the associated estimates to make

⁸The extended model of Adão et al. (2021) features migration, but because it lacks migration costs it does not allow for migration networks that vary by location.

within-sample or counterfactual predictions. It also describes the model-consistent NLLS procedure. Section 4 generalizes the model to include frictions in switching both locations and industries. Section 5 presents the RAIS data and descriptive statistics on worker transitions across locations and industries. Section 6 presents the simulation-based quantitative results, and Section 7 concludes.

2 Simple Model of Mobility with Regional Frictions

2.1 Setup

This section presents a stylized model that yields clear and intuitive expressions for how local labor demand shocks affect local populations in the presence of costly mobility. Although this framework omits a number of potentially empirically relevant mechanisms, including housing, capital markets, and agglomeration economies, it highlights important and general issues with standard regression-based approaches to understanding how changes in local populations respond to local shocks.

Consider a small open economy consisting of many sectors indexed by $n \in \mathcal{N}$ produced in many locations indexed by $\ell \in \mathcal{L}$. Products within a sector are differentiated by location of production. Product markets are frictionless so the price of a sector- n good produced in location ℓ , $p_{\ell n}$, is constant across destinations. Homogeneous labor is the only input, and sector-location productivity is $z_{\ell n}$. Output and labor markets are perfectly competitive, so $p_{\ell n} = w_{\ell}/z_{\ell n}$, where w_{ℓ} is the wage in location ℓ .

Individuals make optimal choices over consumption bundles and their location of employment and face frictions in moving across locations (here, we assume frictionless mobility across industries and add industry-switching frictions in Section 4). We assume that workers may migrate within the country of interest by choosing among locations $\ell \in \mathcal{L}$, but not internationally. Unless explicitly specified otherwise, sums over locations cover only places in the country of interest. Each of L workers inelastically supplies one unit of labor in their chosen location, so changes in employment are equivalent to changes in population. Utility from consumption is Cobb-Douglas across sectors and CES across location-specific varieties within sector:

$$U = \sum_n \eta_n \ln(Q_n), \quad \text{where } Q_n \equiv \left(\sum_{\ell \in \mathcal{L}_w} x_{\ell n}^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}. \quad (2)$$

Note that Q_n aggregates over location-specific varieties produced around the world ($\ell \in \mathcal{L}_w$), including those within the country of interest ($\mathcal{L} \subset \mathcal{L}_w$). Normalizing world aggregate expenditure to one, the aggregate optimal demand bundle satisfies

$$x_{\ell n} = p_{\ell n}^{-\sigma} P_n^{\sigma-1} \eta_n, \quad (3)$$

where $P_n \equiv (\sum_{\ell \in \mathcal{L}_w} p_{\ell n}^{1-\sigma})^{\frac{1}{1-\sigma}}$ is the CES exact price index for sector n , including varieties produced globally. The small-country assumption implies that P_n is set on the world market and is exogenous to developments in the country of interest.

The indirect utility of choosing destination location d for individual i currently living in location ℓ is ⁹

$$V_{i\ell d} = \ln\left(\frac{w_d}{P}\right) - \ln \tau_{\ell d} + \frac{1}{\theta} \epsilon_{id}, \quad (4)$$

where $P \equiv (\Pi_n P_n^{\eta_n}) / (\Pi_n \eta_n^{\eta_n})$ is the Cobb-Douglas exact price index across sectors, $\ln \tau_{\ell d}$ is the utility cost of moving from ℓ to d , and ϵ_{id} is a taste shock following a type-I extreme-value (standard Gumbel) distribution that is i.i.d. across individuals and locations. The parameter θ determines the strength of location preferences relative to the log real wage, with smaller values of θ implying stronger location preference and larger frictions across locations.

2.2 Regional Labor Demand

Given perfectly competitive markets, $p_{\ell n} = w_{\ell}/z_{\ell n}$, and revenue to sector- n producers in location ℓ is

$$R_{\ell n} = \eta_n \left(\frac{w_{\ell}/z_{\ell n}}{P_n}\right)^{1-\sigma}. \quad (5)$$

Perfect competition and regional trade balance imply that the regional wagebill equals total regional revenue across sectors:

$$w_{\ell} L_{\ell} = \sum_n R_{\ell n}. \quad (6)$$

⁹Exogenous local amenities can be incorporated without changing the analysis. Since we do not use data on wages, w_d can be reinterpreted as the amenity-adjusted wage.

Plugging in (5) and rearranging yields regional labor demand:

$$L_\ell = D_\ell w_\ell^{-\sigma}, \quad \text{where } D_\ell \equiv \sum_n \eta_n (z_{\ell n} P_n)^{\sigma-1}. \quad (7)$$

The term D_ℓ is a regional demand shifter affected by changes in productivity $z_{\ell n}$ or industry price indexes P_n . Equation (7) shows that σ is the labor demand elasticity, which is larger when product varieties across locations are more substitutable.

Consider an economic shock that affects this demand shifter across locations in the country of interest.¹⁰ Let hats represent proportional changes relative to a no-shock counterfactual, and assume small changes so $\hat{x} \equiv dx/x = d \ln x$. The total derivative of (7) is then

$$\hat{L}_\ell = \hat{D}_\ell - \sigma \hat{w}_\ell. \quad (8)$$

This expression describes labor demand in location ℓ and can be expressed in matrix notation as

$$\hat{\mathbf{L}} = \hat{\mathbf{D}} - \sigma \hat{\mathbf{w}}. \quad (9)$$

2.3 Regional Labor Supply

Given the assumptions in (4), the probability an individual in location ℓ chooses to live in location d is given by $\pi_{\ell d}$, where

$$\pi_{\ell d} = \frac{(w_d/\tau_{\ell d})^\theta}{\sum_{d'} (w_{d'}/\tau_{\ell d'})^\theta}. \quad (10)$$

We refer to these location-choice probabilities as “out-migration shares.” Equation (10) shows that θ is the migration elasticity reflecting how relative out-migration shares respond to relative wage changes in destination locations; a larger θ implies less variation in the idiosyncratic taste shocks and hence more responsiveness to wage differences. Labor supply to location d is then determined

¹⁰For example, a change to the vector of sectoral price indexes yields a shift-share structure in \hat{D}_ℓ . Differentiating the definition of D_ℓ in (7) yields

$$\hat{D}_\ell = (\sigma - 1) \sum_n \frac{\eta_n (z_{\ell n} P_n)^{\sigma-1} w_\ell^{-\sigma}}{D_\ell w_\ell^{-\sigma}} \hat{P}_n = (\sigma - 1) \sum_n \frac{L_{\ell n}}{L_\ell} \hat{P}_n.$$

by these out-migration shares and the initial distribution of workers across locations, L_ℓ^0 :

$$L_d = \sum_\ell f_{\ell d} = \sum_\ell \pi_{\ell d} L_\ell^0, \quad (11)$$

where $f_{\ell d} \equiv \pi_{\ell d} L_\ell^0$ is the number of people initially in location ℓ who choose location d .

Now consider a labor demand shock leading to small changes in wages across (potentially all) locations, as in (8), while holding moving costs $\tau_{\ell d}$ fixed.¹¹ Totally differentiating (10) and (11) yields

$$\hat{L}_d = \sum_\ell \gamma_{\ell d} \hat{\pi}_{\ell d} = \theta \left(\hat{w}_d - \sum_\ell \gamma_{\ell d} \sum_{d'} \pi_{\ell d'} \hat{w}_{d'} \right). \quad (12)$$

Note that $\gamma_{\ell d} \equiv f_{\ell d}/L_d$ is the share of those in location d who arrived from location ℓ , which we refer to as the “in-migration share.” This expression describes how the quantity of labor supplied in location d responds to wage changes across all destinations and can be written in matrix notation as

$$\hat{\mathbf{L}} = \theta (I - \Gamma' \Pi) \hat{\mathbf{w}}, \quad (13)$$

where Γ is the matrix of in-migration shares ($\gamma_{\ell d}$) and Π is the matrix of out-migration shares ($\pi_{\ell d}$).

2.4 Equilibrium Response to Shocks

Equating the labor demand and labor supply expressions in (9) and (13) and solving yields the equilibrium effects of regional labor demand shocks on regional population and wages:

$$\hat{\mathbf{L}} = (I - \Psi^{-1}) \hat{\mathbf{D}}, \quad (14)$$

$$\hat{\mathbf{w}} = \frac{1}{\sigma} \Psi^{-1} \hat{\mathbf{D}}, \quad (15)$$

where

$$\Psi \equiv \left(1 + \frac{\theta}{\sigma} \right) I - \frac{\theta}{\sigma} \Gamma' \Pi. \quad (16)$$

Equation (14) shows the relationship between population changes and local labor demand shocks, i.e. the relationship whose empirical investigation we seek to inform. Two practical implications

¹¹Appendix A.1 generalizes our results to incorporate both labor demand shocks and labor supply shocks resulting from changes in $\tau_{\ell d}$.

are immediately evident. First, the population change in a given location depends upon the shocks to *all* other locations. In fact, if all locations face the same shock so $\hat{D}_\ell = \hat{D} \forall \ell$, then population in each location remains unchanged.¹² Second, the importance of each shock in changing local population depends upon migrant connections between the focal location and other locations, as reflected in Γ' and Π in Ψ .

To gain intuition for the ways in which these migrant connections influence the effects of shocks on connected regions, consider an approximation in which mobility is low enough that the effects of indirect connections become unimportant. Specifically, write $\Gamma = I + \Delta\Gamma$ and $\Pi = I + \Delta\Pi$ and assume that $\Delta\Gamma'\Delta\Pi \approx \Delta\Gamma'\Delta\Gamma' \approx \Delta\Pi\Delta\Pi \approx \mathbf{0}$. Plugging this into (16) and then (14) yields¹³

$$\hat{L}_\ell \approx \frac{\theta}{\sigma} \left(\sum_o \gamma_{o\ell} (\hat{D}_\ell - \hat{D}_o) + \sum_d \pi_{\ell d} (\hat{D}_\ell - \hat{D}_d) \right). \quad (17)$$

The local shock's effect on local population depends upon how its value compares to shocks facing all other locations, with more weight placed upon shocks in the location's typical migrant sources (captured by $\gamma_{o\ell}$) and its typical migrant destinations (captured by $\pi_{\ell d}$). This expression also shows that when the migration elasticity θ is larger, more individuals choose to migrate in response to a given vector of shocks. Similarly, when the local labor demand elasticity σ is smaller, a given vector of demand shifts leads to larger population changes.

2.5 Linking to Observables

The changes shown in the preceding expressions represent counterfactual differences between situations with and without the labor demand shocks \hat{D} . The migration shares in Γ' and Π are also based on migration flows that would have been observed in the absence of shocks. To make these unobserved counterfactuals equivalent to observable quantities, we assume the economy is initially at steady-state. Specifically, we assume the population in each location was initially stable in period

¹²The goal is to show that $(I - \Psi^{-1})\iota\hat{D} = 0$, where ι is a column vector of ones and \hat{D} is a scalar reflecting the identical shock in all locations. The preceding expression is equivalent to $\Psi^{-1}\iota = \iota$, which in turn implies $\Psi\iota = \iota$. We then use $\Pi\iota = \iota$ and $\Gamma'\iota = \iota$ to show

$$\Psi\iota = \left[\left(1 + \frac{\theta}{\sigma}\right) I - \frac{\theta}{\sigma} \Gamma' \Pi \right] \iota = \left(1 + \frac{\theta}{\sigma}\right) \iota - \frac{\theta}{\sigma} \iota = \iota,$$

which implies zero population change in response to identical shocks in all locations.

¹³Appendix A.2 derives (17).

0, prior to the shock.

$$L_\ell^0 = \sum_o L_o^0 \pi_{o\ell}^0 \quad (18)$$

This assumption implies that in the absence of shocks, the population in each location would remain constant, so the counterfactual difference \hat{L}_ℓ corresponds to the observed change over time. It also implies that the counterfactual migration shares in the absence of shocks equal the observed migration shares from the pre-shock period, i.e. $\pi_{od} = \pi_{od}^0 = f_{od}^0/L_o^0$ and $\gamma_{od} = \gamma_{od}^0 = f_{od}^0/L_d^0$.

We also assume that we do not directly observe the overall labor demand shocks \hat{D} , but instead observe a demand shifter \hat{z} such that

$$\hat{D}_\ell = \hat{z}_\ell + \zeta_{1\ell}, \quad (19)$$

where $\zeta_1 = \{\zeta_{1\ell}\}$ captures unobserved shocks to the local labor market. We assume that the observed demand shocks are as good as random with respect to unobserved shocks, such that

$$\mathbb{E}[\hat{z}_\ell | \zeta_1] = \mu \quad \forall \ell, \quad (20)$$

where μ is a constant (c.f. Borusyak et al. (2022), Assumption 1). In words, the shock to each location has the same mean conditional on all unobserved demand and supply shocks.¹⁴ Combining this formulation with the steady state assumption, the local population change in (14) becomes

$$\hat{\mathbf{L}} = \left(I - (\Psi^0)^{-1} \right) \hat{z} + \zeta_2, \quad (21)$$

where $\zeta_2 = \{\zeta_{2\ell}\}$ is a random error term determined by ζ_1 , and Ψ^0 is calculated using the pre-shock steady-state values of Γ^0 and Π^0 .¹⁵

We can similarly express the low-mobility approximation (17) in terms of observed shocks and pre-shock migration patterns. To aid in proving Theorem 1 below, it is helpful to represent the approximation using a slightly different form than that shown in (17). Letting M_ℓ^0 be the steady-

¹⁴As with any observational research design, the conventional migration regression will yield inconsistent estimates when the shocks are correlated with unobserved determinants of regional population growth. See, for example, Greenland et al. (2019), who argue that the population regression in (Autor et al., 2013) was confounded by pre-existing trends in population growth.

¹⁵Given (19), the error $\zeta_2 \equiv \left(I - (\Psi^0)^{-1} \right) \zeta_1$. In Appendix A.1 we show that it is straightforward to incorporate unobserved labor supply shocks $\nu = \{\nu_\ell\}$ as well, strengthening the shock exogeneity assumption to $\mathbb{E}[\hat{z}_\ell | \zeta_1, \nu] = \mu$.

state number of migrants into or out of location ℓ , i.e. $M_\ell^0 \equiv \sum_{k \neq \ell} f_{k\ell}^0 = \sum_{k \neq \ell} f_{\ell k}^0$, we have

$$\hat{L}_\ell(\hat{\mathbf{z}}) \approx \frac{2\theta}{\sigma} \frac{M_\ell^0}{L_\ell^0} (\hat{z}_\ell - \hat{z}_{-\ell}) + \zeta_{2\ell}, \quad \text{where } \hat{z}_{-\ell} \equiv \sum_{k \neq \ell} \frac{\frac{1}{2} (f_{k\ell}^0 + f_{\ell k}^0)}{M_\ell^0} \hat{z}_k. \quad (22)$$

This expression highlights a number of features that determine how a given vector of shocks affects local population, each of which will be important as we interpret the results of conventional migration regressions in the next section. As discussed above, population responds more strongly when mobility frictions are smaller and labor demand is less elastic, i.e. when θ/σ is larger. Regions with more steady-state migration, i.e. larger M_ℓ^0/L_ℓ^0 , respond more strongly as well. Finally, population responses are larger when the local shock, \hat{z}_ℓ , is larger in comparison to a migration-weighted average of shocks in other regions, $\hat{z}_{-\ell}$.

3 Conventional Regression and Model-Consistent Procedures

The model in the preceding section describes how local populations change in response to labor demand shocks across locations. In this section, we investigate how to interpret the results of conventional migration regressions when the data generating process follows the model just described.

3.1 The Conventional Migration Regression: Defining β

We consider a conventional approach to estimating the impact of labor demand shocks on local population, via Ordinary Least Squares (OLS) regression

$$\hat{L}_\ell = \alpha + \beta \hat{z}_\ell + \varepsilon_\ell, \quad (23)$$

with observations weighted by the pre-period population L_ℓ^0 . The corresponding OLS estimator of β is

$$\hat{\beta} = \frac{\sum_\ell L_\ell^0 \hat{L}_\ell (\hat{z}_\ell - \bar{z})}{\sum_\ell L_\ell^0 (\hat{z}_\ell - \bar{z})^2} \quad (24)$$

where $\bar{z} = \sum_\ell L_\ell^0 \hat{z}_\ell / \sum_\ell L_\ell^0$.¹⁶

We do not assume that equation (23) is correctly specified. Instead, we assume that the data

¹⁶Similar, although more cumbersome, results can be obtained for unweighted regressions used in some studies.

on \hat{L}_ℓ are generated according to the model of Section 2: equation (21) or its approximation (22). We also maintain the assumption that $\{\hat{z}_\ell\}_{\ell \in \mathcal{L}}$ are as-good-as-randomly assigned to regions with respect to all unobserved shocks to labor demand and supply (as in (20)), although they may be mutually correlated in empirical applications (as with shift-share variables).

Since the estimate $\hat{\beta}$ has random variation due to unobserved shocks, we focus on the *estimand* of regression (23), which we define as

$$\beta = \frac{\mathbb{E} \left[\sum_\ell L_\ell^0 \hat{L}_\ell (\hat{z}_\ell - \bar{z}) \right]}{\mathbb{E} \left[\sum_\ell L_\ell^0 (\hat{z}_\ell - \bar{z})^2 \right]}. \quad (25)$$

This expression replaces the numerator and denominator of $\hat{\beta}$ with their expectations taken over observed and unobserved shocks (while viewing the period-0 equilibrium as fixed). This formulation has a number of benefits. First, it applies in finite samples of regions and thus allows us to avoid random sampling assumptions, which are inappropriate in typical applications including all regions of the country. Second, as we show in Appendix A.3, β approximates the probability limit of $\hat{\beta}$ in an asymptotic sequence of economies with growing numbers of regions, under appropriate regularity conditions. That is, in large samples where the impact of the unobserved shocks on $\hat{\beta}$ vanishes, we expect $\hat{\beta} \approx \beta$. Third, unlike $\mathbb{E} [\hat{\beta}]$, the formulation in (25) is analytically tractable, which allows for the convenient characterization presented in the following subsection.

3.2 Characterizing β

We now characterize β when the data were generated by the model described in Section 2. To make the results intuitively interpretable, we focus throughout on the low-mobility approximation to \hat{L}_ℓ , shown in (22).

To understand our characterization, it is helpful to define some notation. Let $M^0 \equiv \sum_{o \neq d} f_{od}^0$ be the steady-state total number of migrants in the country of interest, observed in the pre-shock period, so M^0/L^0 is the steady-state migrant share of the population. We then define similar quantities that would prevail if the observed local populations reflected the steady-state in an economy with no migration costs, i.e. if $\tau_{od} = 1 \forall o, d$. Without migration costs, the steady-state probability of moving to any destination will equal the destination's share of national population, regardless of the

origin.¹⁷ Define $\tilde{f}_{od}^0 \equiv L_o^0 \cdot \frac{L_d^0}{L^0}$ as the number of migrants from o to d and $\tilde{M}^0 \equiv \sum_{o \neq d} \tilde{f}_{od}^0$ as the total number of migrants in this costless-migration setting. The following theorem then characterizes β estimated with data generated by the model.

Theorem 1. *Suppose the data are generated by the low-mobility approximation (22) and the shocks are homoskedastic, i.e. $\text{Var}[\hat{z}_\ell]$ is the same for all ℓ . Then*

$$\beta = \frac{2\theta}{\sigma} \cdot \frac{M^0/L^0}{\tilde{M}^0/L^0} \cdot \frac{1-\rho}{1-\tilde{\rho}}, \quad (26)$$

where $\rho = \sum_{o \neq d} \frac{f_{od}^0}{M^0} \text{Corr}[\hat{z}_o, \hat{z}_d]$ is the average correlation between shocks to pairs of distinct regions weighted by migration flows and $\tilde{\rho} = \sum_{o \neq d} \frac{\tilde{f}_{od}^0}{\tilde{M}^0} \text{Corr}[\hat{z}_o, \hat{z}_d]$ is a similar shock correlation weighted by the flows in the no-migration-cost scenario.

Appendix A.4 proves this result, along with its generalization to heteroskedastic shocks.

Equation (26) shows that β can be viewed as a product of several factors with distinct economic meanings. First, β depends on the structural *elasticities*: as discussed above, true migration responses are larger when θ is large or σ is small, and β inherits those relationships. Second, β increases with the national migration *share* M^0/L^0 (the term \tilde{M}^0/L^0 is generally close to one and can therefore be ignored in practice).¹⁸ Third, β is smaller when $\rho > \tilde{\rho}$; that is, if shocks are particularly positively correlated between regions with large migration flows (i.e. flows that exceed those one would expect based solely on location sizes)—for instance, if migration is more likely at close geographic distances and shocks exhibit spatial correlation. We call the term $\frac{1-\rho}{1-\tilde{\rho}}$ the *attenuation factor*: it reflects how the mutual correlation of shocks along the migration network attenuates the OLS coefficient. When shocks to migrant-connected locations are strongly correlated, individuals have minimal incentive to migrate, so we observe minimal migration response and estimate a relatively small (attenuated) value of β .

¹⁷When $\tau_{\ell d} = 1 \forall \ell, d$, (10) implies that the share of individuals choosing destination d does not depend on source ℓ : $\pi_{\ell d} = w_d^0 / \sum_{d'} w_{d'}^0 \equiv \pi_d$. In steady state, $L_d^0 = \sum_{\ell} \pi_{\ell d} L_\ell^0 = \pi_d L$, so $\pi_d = L_d^0 / L$, i.e. the probability of choosing d equals d 's share of national population. This in turn implies that the steady-state flow of individuals from ℓ choosing d is $\pi_{\ell d} L_\ell = \pi_d L_\ell = L_\ell L_d / L$.

¹⁸Specifically, $\frac{\tilde{M}^0}{L^0} = 1 - \sum_{\ell} \frac{\tilde{f}_{\ell\ell}^0}{L^0} = 1 - \sum_{\ell} \left(\frac{L_\ell^0}{L^0} \right)^2$ equals one minus the Herfindahl index of population across regions. The Herfindahl index is small when the number of regions is sufficiently large and population is not too concentrated in a small number of them, as in our data.

3.3 What Do We Learn from β ?

The expression for β in Theorem 1 reveals how one can and cannot interpret estimates from conventional migration regressions. Here, we will consider various potential interpretations and compare them to correct interpretations in light of the model. To be precise about the causal effects of interest, we will refer to $\hat{L}_\ell(\hat{\mathbf{z}})$, the model-predicted population growth in ℓ under shock vector $\hat{\mathbf{z}}$, defined in equation (22).¹⁹ $\hat{L}_\ell(\hat{\mathbf{z}})$ depends on the entire shock vector $\hat{\mathbf{z}}$, not just the direct shock to ℓ , as reflected in the presence of both \hat{z}_ℓ and $\hat{z}_{-\ell}$ in (22). To analyze counterfactual shocks, we denote a vector $\hat{\mathbf{z}}$ whose ℓ^{th} element has been changed from \hat{z}_ℓ to the scalar value a by $(\hat{\mathbf{z}} \stackrel{\ell}{\leftarrow} a) \equiv (\hat{z}_1, \dots, \hat{z}_{\ell-1}, a, \hat{z}_{\ell+1}, \dots, \hat{z}_n)$.

Effect of a shock to a single location. Researchers often use β to infer the causal effect of a labor demand shock to a single location on that location’s population. A common approach interprets β as the effect of a unit labor demand shock to location ℓ on ℓ ’s population, implicitly fixing other locations’ labor demand shocks at zero. Equation (22) shows that the true causal effect is $\hat{L}_\ell(\mathbf{0} \stackrel{\ell}{\leftarrow} 1) - \hat{L}_\ell(\mathbf{0}) = \frac{2\theta}{\sigma} \frac{M_\ell^0}{L_\ell^0}$. The estimate of β in (26) differs from this model-implied population growth in two important ways. First, it misses location-specific heterogeneity in the effect of a local shock; the model-implied population growth depends on the location-specific migration share $\frac{M_\ell^0}{L_\ell^0}$, while the regression estimate depends on the national migration share $\frac{M^0}{L^0}$ (recall $\frac{\widetilde{M}^0}{L^0} \approx 1$). As we will see in Section 5.2, local migration shares often vary substantially, so this heterogeneity can be important in practice.²⁰

Second, the estimate of β includes the attenuation factor $\frac{1-\rho}{1-\rho}$ resulting from the correlation in shocks among locations with strong migrant connections. Because of this attenuation factor, a researcher may estimate a small value of β that is statistically indistinguishable from zero even when a shock to any single location would actually lead to a substantial migration response. Consistent with this analysis, Section 6 shows that β substantially understates the true effect of a unit shock to a single location in a realistic empirical setting.

The same analysis and conclusions apply to other interpretations of β involving the effect of a shock to a single location. Examples include i) interpreting $\beta\hat{z}_\ell$ as the effect of the observed shock to

¹⁹Note that $\hat{L}_\ell(\hat{\mathbf{z}})$ includes the effect of unobserved shocks, so $\hat{L}_\ell(\mathbf{0}) = \zeta_{2\ell}$.

²⁰This problem would not arise if the outcome variable of the regression was the net population change divided by the initial gross migration flow M_ℓ rather than divided by the initial population.

ℓ , holding all other locations' shocks fixed at their observed values, ii) interpreting $\beta(\hat{z}_k - \hat{z}_\ell)$ as the difference in population growth caused by the difference in observed shocks across locations k and ℓ , and iii) interpreting $\beta(\hat{z}^{p75} - \hat{z}^{p25})$ as the effect of an arbitrary change in the shocks to location ℓ , say from the 25th to the 75th percentile of the shock distribution. All of these cases suffer from the same problems as the unit shock discussed above: the regression-based prediction omits local heterogeneity in migration intensity and suffers from attenuation resulting from correlated shocks across migrant-connected locations.²¹

Effect of shocks to all locations. A problem with all of the preceding interpretations is that they consider counterfactuals that change the shock value in a single location. This approach is at odds with equation (22), in which shocks to *all* locations affect the true population growth in a given location. We therefore consider the effect of the entire observed shock vector $\hat{\mathbf{z}}$ on population growth in each location ℓ , i.e. $\hat{L}_\ell(\hat{\mathbf{z}}) - \hat{L}_\ell(\mathbf{0}) = \frac{2\theta}{\sigma} \frac{M_\ell^0}{L_\ell^0} (\hat{z}_\ell - \hat{z}_{-\ell})$.

It is important to note that the (population-weighted) average effect of any shock vector $\hat{\mathbf{z}}$ is zero by construction, since national population is assumed to be unaffected by the shock.²² A meaningful interpretation of β must therefore involve comparisons across locations. To see why, consider using $\beta\hat{z}_\ell$ to predict the shock vector's effect on population growth in each location ℓ . In many empirical contexts, the shocks to all locations have the same sign, so $\beta\hat{z}_\ell$ would incorrectly imply either population growth in all locations or population declines in all locations. A more sensible approach attributes to the local shock only its effect relative to the mean, $\beta(\hat{z}_\ell - \bar{z})$. This approach ensures that the predicted effects of the shocks average to zero across locations and is consistent with the inclusion of an intercept term α in the conventional regression (23). It also yields the best (mean squared error (MSE) minimizing) prediction of the expected population growth in location ℓ among linear functions of $(\hat{z}_\ell - \bar{z})$.²³

²¹In case i) the true effect is $\hat{L}_\ell(\hat{\mathbf{z}}) - \hat{L}_\ell(\hat{\mathbf{z}} \leftarrow 0) = \frac{2\theta}{\sigma} \frac{M_\ell^0}{L_\ell^0} \hat{z}_\ell$, while the regression-based prediction is $\beta\hat{z}_\ell = \frac{2\theta}{\sigma} \cdot \frac{M^0/L^0}{M^0/L^0} \cdot \frac{1-\rho}{1-\rho} \hat{z}_\ell$. In case ii) one potential formalization is the effect on location ℓ 's population of changing ℓ 's shock from \hat{z}_ℓ to \hat{z}_k , fixing other locations' shocks at their observed values. The true effect of this change is $\hat{L}_\ell(\hat{\mathbf{z}} \leftarrow \hat{z}_k) - \hat{L}_\ell(\hat{\mathbf{z}}) = \frac{2\theta}{\sigma} \frac{M_\ell^0}{L_\ell^0} (\hat{z}_k - \hat{z}_\ell)$, while the regression-based prediction is $\beta(\hat{z}_k - \hat{z}_\ell) = \frac{2\theta}{\sigma} \cdot \frac{M^0/L^0}{M^0/L^0} \cdot \frac{1-\rho}{1-\rho} (\hat{z}_k - \hat{z}_\ell)$. In case iii) the true effect is $\hat{L}_\ell(\hat{\mathbf{z}} \leftarrow \hat{z}^{p75}) - \hat{L}_\ell(\hat{\mathbf{z}} \leftarrow \hat{z}^{p25}) = \frac{2\theta}{\sigma} \frac{M_\ell^0}{L_\ell^0} (\hat{z}^{p75} - \hat{z}^{p25})$, while the regression-based prediction is $\beta(\hat{z}^{p75} - \hat{z}^{p25}) = \frac{2\theta}{\sigma} \cdot \frac{M^0/L^0}{M^0/L^0} \cdot \frac{1-\rho}{1-\rho} (\hat{z}^{p75} - \hat{z}^{p25})$.

²²This assumption can be relaxed by allowing for international migration and introducing one or more additional locations representing foreign destinations and incorporating these into the analysis.

²³We do not assume *iid* shocks across locations, which makes our results applicable to shift-share research designs.

However, using $\hat{z}_\ell - \bar{z}$ alone to predict local population growth is likely to yield very poor predictions. To see why, use the decomposition of β in (26) to write

$$\beta(\hat{z}_\ell - \bar{z}) = \frac{2\theta}{\sigma} \cdot \frac{M^0/L^0}{\widetilde{M^0/L^0}} \left((\hat{z}_\ell - \bar{z}) - \frac{\rho - \tilde{\rho}}{1 - \tilde{\rho}} \cdot (\hat{z}_\ell - \bar{z}) \right). \quad (27)$$

Compare this prediction to (22), the model's expected population growth in ℓ when facing the observed vector of demeaned shocks: $\frac{2\theta}{\sigma} \cdot \frac{M_\ell^0}{L_\ell^0} ((\hat{z}_\ell - \bar{z}) - (\hat{z}_{-\ell} - \bar{z}))$. The estimate $\beta(\hat{z}_\ell - \bar{z})$ omits two key sources of variation. As before, it omits heterogeneity based on the local migration intensity, $\frac{M_\ell^0}{L_\ell^0}$. Even more importantly, it replaces the shocks to other migration-connected locations, $(\hat{z}_{-\ell} - \bar{z})$, with the scaled local shock relative to the mean $\frac{\rho - \tilde{\rho}}{1 - \tilde{\rho}} (\hat{z}_\ell - \bar{z})$. Shocks to other locations are important drivers of local population change according to the model and can differ substantially among locations facing similar direct shocks, but this information is omitted from (27). Because the fitted values from the population regression only use information on the direct shocks to the location, they cannot account for the extent to which other migrant sources and destinations faced similar or different shocks. As we will see in Section 5.2, the omission of these cross-location spillover effects can be quantitatively important.

Rather than attempting to use β to predict the effect of $\hat{\mathbf{z}}$ on one location's population growth, an alternative approach would interpret $\beta(\hat{z}_k - \hat{z}_\ell)$ as the difference in the effects of all shocks between particular locations k and ℓ .²⁴ This interpretation suffers from similar problems to those already discussed: it omits heterogeneity in migration intensity and fails to account for the particular differences between migrant-connected shocks \hat{z}_{-k} and $\hat{z}_{-\ell}$.²⁵ Yet, there is a valid interpretation based on the *average* difference in effects of all shocks between locations facing different direct shocks (Choi, 2022). The most straightforward way to demonstrate this interpretation is to consider the following regression, which relates the effect of all shocks on population growth in location ℓ to

See Appendix A.5 for a proof that $\beta(\hat{z}_\ell - \bar{z})$ yields the MSE-minimizing predicted population growth in this setting.

²⁴This interpretation considers the difference between locations k and ℓ in the effect of *all* shocks relative to a counterfactual of zero shock in *all* locations: $(\hat{L}_k(\hat{\mathbf{z}}) - \hat{L}_k(\mathbf{0})) - (\hat{L}_\ell(\hat{\mathbf{z}}) - \hat{L}_\ell(\mathbf{0}))$. Interpretation ii) in footnote 21 considers the effect of changing location ℓ 's shock from \hat{z}_ℓ to \hat{z}_k , while holding all other locations' shocks fixed: $\hat{L}_\ell(\hat{\mathbf{z}} \xleftarrow{\ell} \hat{z}_k) - \hat{L}_\ell(\hat{\mathbf{z}})$.

²⁵The difference in the effects of all shocks $\hat{\mathbf{z}}$ between locations k and ℓ is

$$(\hat{L}_k(\hat{\mathbf{z}}) - \hat{L}_k(\mathbf{0})) - (\hat{L}_\ell(\hat{\mathbf{z}}) - \hat{L}_\ell(\mathbf{0})) = \frac{2\theta}{\sigma} \left[\left(\frac{M_k^0}{L_k^0} \hat{z}_k - \frac{M_\ell^0}{L_\ell^0} \hat{z}_\ell \right) - \left(\frac{M_k^0}{L_k^0} \hat{z}_{-k} - \frac{M_\ell^0}{L_\ell^0} \hat{z}_{-\ell} \right) \right].$$

$\beta(\hat{z}_k - \hat{z}_\ell)$ omits heterogeneity based on initial migration intensity and captures the differences in \hat{z}_{-k} and $\hat{z}_{-\ell}$ using only $(\hat{z}_k - \hat{z}_\ell)$.

location ℓ 's direct shock:

$$\hat{L}_\ell(\hat{\mathbf{z}}) - \hat{L}_\ell(\mathbf{0}) = a + b\hat{z}_\ell + e_\ell. \quad (28)$$

The regression coefficient b in this specification captures the average difference in the effect of all shocks, $\hat{\mathbf{z}}$, in places facing different direct shocks, \hat{z}_ℓ . Here b can not be estimated directly, since the dependent variable is not observable. However, since $\hat{L}_\ell(\hat{\mathbf{z}})$ is the observed population change given the realized shocks $\hat{\mathbf{z}}$, the only difference between the specification in (28) and the conventional migration regression in (23), is the inclusion of $\hat{L}_\ell(\mathbf{0})$ on the left side of (28). Yet, the as-good-as-random assumption regarding \hat{z}_ℓ in equation (20) implies that \hat{z}_ℓ is orthogonal to $\hat{L}_\ell(\mathbf{0})$, so the β and b estimands are equal. We can therefore accurately interpret an estimate of β as the average difference in the effect of all shocks between places facing a unit difference in direct local shock. Importantly, this interpretation only holds for the realized shocks used to estimate β . Counterfactual shock vectors will generally induce different correlation structures across migrant-connected regions that will not be captured by β estimated using the realized shocks.

To summarize, an estimate of β from the conventional migration regression in (23) does not yield accurate predictions regarding the causal effects of observed or counterfactual shocks to particular individual locations or differences in effects across particular pairs of locations. For example, the estimate of β may be close to zero even when a counterfactual shock to a single location would drive substantial migration. While β does identify the difference in the average effect of the entire vector of shocks on regions that face higher vs. lower direct shocks, this interpretation is limited. A counterfactual vector of shocks of similar magnitude to the observed shocks but with a different correlation structure may yield very different migration responses. We learn little about interregional mobility costs or migration elasticities from an estimate of β and should therefore not use results from conventional migration regressions to justify model restrictions or to calibrate model parameters.

Confounding migration in wage regressions. Some analyses estimate the conventional migration regression in (23) not to draw conclusions about the effects of shocks on local populations, but to assess whether interregional migration is likely to substantially affect estimates of the effect of local shocks on local economic outcomes such as wages. Appendix A.6 examines this approach in light of the model, finding that when the conventional regression estimate of β is close to zero, wage

regression estimates will experience minimal confounding, irrespective of the mechanism driving the small estimate of β . In other words, even if the estimate of β is close to zero due to correlated shocks across migrant-connected locations, a regression of local wage growth on as-good-as-random local labor demand shocks will still yield an estimate that is close to the inverse labor demand elasticity, $1/\sigma$.

3.4 A Model-Consistent Specification

We now describe an alternative empirical approach that integrates information on regional shocks and pre-shock migration patterns to estimate migration responses in a way that is consistent with the model. The model-implied relationship between local population changes and the vector of local labor demand shocks is given by equation (21) above, rearranged slightly here.

$$\hat{\mathbf{L}} = \left(I - \Psi^0(\theta/\sigma)^{-1} \right) \hat{\mathbf{z}} + \zeta_2, \quad (29)$$

$$\text{where } \Psi^0(\theta/\sigma) \equiv \left(I + \frac{\theta}{\sigma} (I - \Gamma^{0'} \Pi^0) \right).$$

We observe the population change $\hat{\mathbf{L}}$, the pre-shock migration matrices $\Gamma^{0'}$ and Π^0 , and the shocks $\hat{\mathbf{z}}$, so we can estimate the parameter θ/σ using non-linear least squares (NLLS).²⁶ Formally, in Appendix A.8 we show that whenever $\hat{\mathbf{z}}$ has a non-degenerate variance-covariance matrix, $\frac{\theta}{\sigma}$ uniquely solves the NLLS problem²⁷

$$\min_{\lambda} \mathbb{E} \left[\left(\hat{\mathbf{L}} - (I - \Psi^0(\lambda)^{-1}) \hat{\mathbf{z}} \right)' \left(\hat{\mathbf{L}} - (I - \Psi^0(\lambda)^{-1}) \hat{\mathbf{z}} \right) \right]. \quad (30)$$

Given the resulting estimate of θ/σ we can calculate shock-induced population changes in each location using the same relationship in (29), omitting the error term. This process can be used to predict internally valid effects of the observed shocks used to estimate θ/σ in (29) and externally valid effects of counterfactual shocks.

²⁶We recommend an intercept is included in equation (29) in practice to capture exogenous changes in national population (due to population growth or international migration) and increase estimation efficiency.

²⁷Borusyak and Hull (2021, Appendix D.5) show in a similar setting that a “recentering” adjustment is generally necessary for the appropriate moment condition to hold under the as-good-as-random assignment of the shocks, $\mathbb{E}[\hat{z}_\ell | \zeta_1] = \mu$. We show in Appendix A.7 that this issue does not arise in our setting because NLLS estimates are invariant to μ : demeaning the shock has no implications for population changes. Recentering would be necessary, however, if the shocks were *conditionally* as-good-as-randomly assigned: e.g. higher in regions with a higher manufacturing employment share, as in many empirical settings (e.g. Autor et al. (2013)).

Two caveats should be kept in mind here. First, we assume that the researcher has available a set of shocks to local labor demand that are as good as randomly assigned (as in (20)) with which to estimate θ/σ . Any endogeneity in the shocks will lead to inconsistency in both the proposed NLS procedure and the conventional migration regression. Second, our model is purposefully stylized in order to focus on the conventional migration regression’s failure to account for shocks to other migrant-connected locations. The model does not include other mechanisms such as agglomeration economics, housing, and capital markets. Instead, our relatively parsimonious model focuses on the the cross-location spillover problem facing conventional migration regressions.

4 Extension to Frictional Labor Mobility across Industries

The model described in the preceding section allows for frictions in moving across locations, but assumes costless mobility across industries within a given location. Here, we extend the model to allow for costly mobility across both industries and locations by applying the same analysis at the location-industry level. For example, the indirect utility in (4) can be written identically, but with the subscript ℓ referring to the worker’s current location-industry pair and d referring to the location-industry pair that the worker might choose. It will be helpful to make this distinction explicit by defining the initial location and industry as ℓ and n and the new location and industry as d and q . To clarify the distinction between prior and current location-industry information, we separate the subscripts with a comma. Workers face a moving cost $\tau_{\ell n, dq}$ when switching from location-industry pair ℓn to pair dq , and θ determines the responsiveness of labor supply between one location-industry pair and another. Note that, for simplicity, this setup assumes that the same parameter θ applies to both the location and industry dimensions.²⁸

The model extends directly to the location-industry context, and we again make use of the low-mobility approximation to derive an intuitive expression relating labor demand shocks to population

²⁸As discussed in footnote 39, available estimates suggest that θ is similar across locations and industries, supporting the restriction of a single parameter in both dimensions.

changes at the location-industry level.²⁹ Applying (17) and (19) in that setting yields

$$\hat{L}_{\ell n} \approx \frac{\theta}{\sigma} \left(\sum_{o \in \mathcal{L}} \sum_{p \in \mathcal{N}} \gamma_{op, \ell n}^0 (\hat{z}_{\ell n} - \hat{z}_{op}) + \sum_{d \in \mathcal{L}} \sum_{q \in \mathcal{N}} \pi_{\ell n, dq}^0 (\hat{z}_{\ell n} - \hat{z}_{dq}) \right) + \zeta_{\ell n}, \quad (31)$$

where $\gamma_{op, \ell n}^0 = f_{op, \ell n}^0 / L_{\ell n}^0$ is the share of workers in location-industry cell ℓn who came from cell op in the pre-shock steady state, $\pi_{\ell n, dq}^0 = f_{\ell n, dq}^0 / L_{\ell n}^0$ is the share of workers in cell ℓn who went to cell dq , the $\hat{z}_{\ell n}$ are observable labor demand shocks in cell ℓn , and $\zeta_{\ell n}$ is an error term such that $\mathbb{E}[\hat{z}_{\ell n} | \boldsymbol{\zeta}] = \mu$, $\forall \ell, n$ as in (20).

This model allows us to interpret the conventional location-level migration regression when the data reflect a setting with frictions across both industries and locations. The conventional regression remains identical to equation (23), where we aggregate across industries to yield the location's change in population $\hat{L}_\ell = \sum_n \frac{L_{\ell n}^0}{L_\ell^0} \hat{L}_{\ell n}$ and the location's average labor demand shock $\hat{z}_\ell \equiv \sum_n \frac{L_{\ell n}^0}{L_\ell^0} \hat{z}_{\ell n}$.

To illustrate the regional population responses in this more general model, we contrast scenarios in which the shocks are purely regional vs. purely industry-level. In the case of purely regional shocks, i.e. when $\hat{z}_{\ell n} = \hat{x}_\ell \forall \ell, n$, we find population responses that are identical to those in the model with regional frictions alone, and therefore the same problems arise. Simplifying equation (31) yields

$$\begin{aligned} \hat{L}_\ell &\approx \frac{\theta}{\sigma} \left(\sum_{n \in \mathcal{N}} \sum_{o \in \mathcal{L}} \sum_{p \in \mathcal{N}} \frac{f_{op, \ell n}^0}{L_\ell^0} (\hat{x}_\ell - \hat{x}_o) + \sum_{n \in \mathcal{N}} \sum_{d \in \mathcal{L}} \sum_{q \in \mathcal{N}} \frac{f_{\ell n, dq}^0}{L_\ell^0} (\hat{x}_\ell - \hat{x}_d) \right) + \zeta_\ell \\ &= \frac{\theta}{\sigma} \left(\sum_{o \in \mathcal{L}} \frac{f_{o, \ell}^0}{L_\ell^0} (\hat{x}_\ell - \hat{x}_o) + \sum_{d \in \mathcal{L}} \frac{f_{\ell, d}^0}{L_\ell^0} (\hat{x}_\ell - \hat{x}_d) \right) + \zeta_\ell, \end{aligned} \quad (32)$$

where $\zeta_\ell \equiv \sum_n \frac{L_{\ell n}^0}{L_\ell^0} \zeta_{\ell n}$. This expression is identical to (17) in the model with location frictions only (expressed using the observable component of the regional labor demand shocks $\hat{\mathbf{x}}$ rather than the overall shocks $\hat{\mathbf{D}}$). Because the two situations imply the same population changes (given the low-mobility approximation), they imply the same values for β in the conventional migration regression. In other words, when the shock is purely regional, the presence of industry frictions does not alter

²⁹Note that the low-mobility approximation may perform more poorly in the location-industry context, since there may be substantial mobility across industries within location.

migration behavior, and all of the problems of interpretation discussed in Section 3.3 apply to the model with location and industry frictions.³⁰

While purely regional shocks yield identical migration behavior in the models with and without industry switching frictions, the two models yield very different results with purely industry-level labor demand shocks, i.e. when $\hat{z}_{\ell n} = \hat{x}_n \forall \ell, n$. In a regional migration analysis, researchers typically incorporate industry-level shocks using a shift-share structure, in which the average shock facing workers in location ℓ is an employment-weighted average of industry shocks: $\hat{z}_\ell = \sum_n \frac{L_{\ell n}^0}{L_\ell^0} \hat{x}_n$. When switching industries is costless, as in the baseline model of Section 2, this shift-share measure captures the regional labor demand shock facing all workers in location ℓ , i.e. the shift-share measure *is* the regional labor demand shock. In contrast, when industry switching frictions are present, workers in the same location but in different industries experience different labor demand changes and have different incentives to migrate. We therefore find distinct migration behavior in models with and without industry frictions when facing industry-level labor demand shocks.

We formalize this intuition by plugging the assumption $\hat{z}_{\ell n} = \hat{x}_n \forall \ell, n$ into (31) and simplifying.

$$\begin{aligned} \hat{L}_\ell &\approx \frac{\theta}{\sigma} \left(\sum_{n \in \mathcal{N}} \sum_{o \in \mathcal{L}} \sum_{p \in \mathcal{N}} \frac{f_{op, \ell n}^0}{L_\ell^0} (\hat{x}_n - \hat{x}_p) + \sum_{n \in \mathcal{N}} \sum_{d \in \mathcal{L}} \sum_{q \in \mathcal{N}} \frac{f_{\ell n, dq}^0}{L_\ell^0} (\hat{x}_n - \hat{x}_q) \right) + \zeta_\ell \\ &= \frac{2\theta}{\sigma} \left(\hat{z}_\ell - \frac{1}{2} \sum_{p \in \mathcal{N}} \frac{f_{p, \ell}^0}{L_\ell^0} \hat{x}_p - \frac{1}{2} \sum_{q \in \mathcal{N}} \frac{f_{\ell, q}^0}{L_\ell^0} \hat{x}_q \right) + \zeta_\ell, \end{aligned} \quad (33)$$

where $f_{p, \ell}^0$ is the number of workers in location ℓ who previously worked in industry p , and $f_{\ell, q}^0$ is the number of workers previously in location ℓ currently working in industry q . In this case, migration is determined by the difference between the shift-share shock facing location ℓ , \hat{z}_ℓ , and the average shocks facing the former industries of workers in that location, $\sum_p \frac{f_{p, \ell}^0}{L_\ell^0} \hat{x}_p$, and those facing the current industries of workers who were previously in that location, $\sum_q \frac{f_{\ell, q}^0}{L_\ell^0} \hat{x}_q$.

To illustrate the implications of (33) for migration behavior, consider an extreme scenario in which workers can not switch industries, formalized by $\tau_{\ell n, dm} = \infty$ for all ℓ, d , and $n \neq m$. In that case, although regional shocks will induce migration as in (32), pure industry shocks will not. Because workers can not change industries, those migrating to or from ℓ in steady-state will have

³⁰This conclusion applies to any location-specific shock irrespective of its source or level of aggregation. This includes state-level shocks that are common to many locations.

the same industry mix as those in ℓ , so the terms on the right hand side of (33) cancel out, and $\hat{L}_\ell = 0 \forall \ell$. Thus, in this scenario, β will be positive for regional shocks but zero for industry shocks. This extreme example illustrates the more general point that industry-switching frictions reduce migration responses when labor demand shocks have an industry-specific component. Intuitively, if switching industries is difficult, workers see less benefit in moving to a location with a more favorably affected industry mix because they would still face much of their original industry's shock in the new location.

Given the migration behavior implied by (33), how can we interpret the results of the conventional migration regression? Consider interpreting β as the effect of a counterfactual unit labor demand shock in a single location on that location's population. As just discussed, the regression estimate will be even further attenuated than in the purely regional context by the presence of industry-switching costs, since industry frictions disincentivize regional mobility when facing industry-level shocks. Using β to estimate the effect of the observed shocks on regional populations is similarly problematic for reasons that parallel those discussed in Section 3.3. The conventional migration regression uses the regional shift-share measure \hat{z}_ℓ alone to estimate its direct effect in location ℓ and the spillover effect of the complex averages of shocks in the former and subsequent industries of the location's workers shown in (33). As the simulations in Section 6 will reveal, these estimates will be even less accurate than those in a context with regional frictions alone (and, therefore, regional shocks).

This discussion reveals how industry frictions undermine the intuitive appeal of measuring local labor demand shocks using shift-share measures. Only when industry frictions are absent does the industry shift-share represent a true regional labor demand shock facing all local workers. With industry frictions, workers in different industries face different shocks and have different outside options, leading to complex spillovers of the effects of shocks across industries and regions. Yet, all of these complexities are omitted by the conventional migration regression, exacerbating the biases examined in Section 3.3.

5 Data and Descriptive Statistics

To assess the practical importance of the conceptual problems with the conventional migration regression that we have discussed in Sections 2 through 4, we now examine these issues empirically using data on observed worker transitions across locations and industries.

5.1 Data

The NLLS approach described in Section 3.4 and the model simulations presented in Section 6 require information on worker transitions across locations or across location-industry pairs, allowing us calculate the steady-state transition matrices Γ^0 and Π^0 . We do so using administrative panel data covering all formally employed workers in Brazil, allowing us to observe these detailed transitions across locations and industries. Subsequent revisions will present results using similar data in other countries.

We utilize data from the *Relação Anual de Informações Sociais* (RAIS) covering 1994 to 2000. This administrative dataset is a census of the Brazilian formal labor market that allows us to follow all formally employed workers across jobs in different industries and locations (De Negri et al., 2001; Saboia and Tolipan, 1985).³¹ Locations in our analysis are based on the “microregion” definition of the Brazilian Statistical Agency (IBGE, 2002), which combines economically integrated contiguous municipalities (counties) with similar geographic and productive characteristics. We aggregate microregions slightly to ensure consistent boundaries over time, following Dix-Carneiro and Kovak (2017), yielding 486 time-consistent microregion locations in Brazil’s 27 states.³² Industries are based on the “Subsetor IBGE” classification the RAIS dataset uses to identify the industry associated with each employer. This classification identifies 25 distinct industries including 12 manufacturing industries.

Our sample includes individuals age 18 to 64 with positive earnings in December of the relevant year.³³ We also drop individuals with missing or inconsistent information, including “other/ignored”

³¹Formality is defined as having a signed work card (*carteira assinada*) registering their contract with the Ministry of Labor and giving workers the right to benefits and protections of the legal employment system. The restriction to formal workers is important in the Brazilian context, as informality rates measured in the Brazilian Census exceed 50% during our sample period (Dix-Carneiro and Kovak, 2019).

³²As Dix-Carneiro and Kovak (2017) report using Census data, only 3.4 percent of individuals lived and worked in different microregions in the year 2000, so the microregion of employment is a quite accurate measure of both employment and residence location.

³³RAIS reports earnings for December and average monthly earnings during employed months in the reference year.

industries, contradictory education levels across jobs in the same year, holding jobs in very distant geographic areas, etc. If a worker holds multiple jobs, we select the job with the highest December earnings and use it to assign the worker’s location and industry of employment. When examining differences by skill level, we define skilled workers as those with a high school degree or more and unskilled workers as those without a high school degree.

In the context of the model with full employment and no labor supply decision, there is no distinction between changes in population and changes in employment. The RAIS data allow us to observe formal employment in location-industry pairs and transitions between them, but do not provide any information on non-employed or informally employed individuals. We therefore use the RAIS data to calculate yearly formally-employed worker flows between location-industry pairs, omitting transitions into or out of formal employment. Because we use detailed geographic and industry information, workers may transition between $12,150 = 486 \times 25$ location-industry cells. Consistent with the steady-state assumption and to reduce noise in estimating transitions between small cells, we average the observed yearly flows between each location-industry cell from 1994 to 2000 and use these averages to calculate migration flows, employment levels, and employment changes both at the location and location-industry levels.³⁴

5.2 Descriptive Evidence

Table 1 reports average yearly mobility rates between locations (microregions), between the 27 Brazilian states, between industries, and between locations and industries. 4.2 percent of workers migrate across locations in a given year on average. Industry transitions are more common than migration events, and workers are much more likely to move across locations within states than across states. Low-skilled workers are slightly more likely to migrate than are high-skilled workers, but are less likely to switch industries. We also find substantial heterogeneity in migration rates across locations. Figure 1 shows a histogram of M_ℓ^0/L_ℓ^0 , the share of individuals in ℓ who move to a different location in a typical year (weighted by the region’s initial employment). As discussed in Section 3.3, this heterogeneity in baseline migration intensity is important because it drives

We use December earnings to ensure that our results are not influenced by seasonal variation or month-to-month inflation.

³⁴Specifically, define $f_{\ell n, dq}^{t, t+1}$ as the observed the number of workers moving from cell ℓn to cell dq between year t and $t + 1$. Then calculate the average across years as $\bar{f}_{\ell n, dq} \equiv \frac{1}{6} \sum_{t=1994}^{1999} f_{\ell n, dq}^{t, t+1}$. These average flows are then aggregated to measure the initial employment levels, local industry compositions, and transition matrices.

Table 1: Average Mobility Rates, %

Across	All Workers	High-Skilled	Low-Skilled
Locations	4.2	4.2	4.3
States	0.9	0.8	1.0
Industries	8.0	8.3	7.5
Locations and Industries	1.3	1.3	1.2

Notes: Percent of individuals with yearly transitions between the cells defined in the first column, calculated from average yearly flows between location-industry cells in RAIS data from 1994 to 2000 as described in footnote 34. The last row measures the fraction of workers who change *both* location and industry in the same year. High-skilled is defined as having a high-school degree or more and low-skilled as less than high school.

heterogeneity in the true effect of local labor demand shocks on local population (as in (22)), but this heterogeneity is omitted from the estimate of β in the conventional migration regression (as in (26)).³⁵

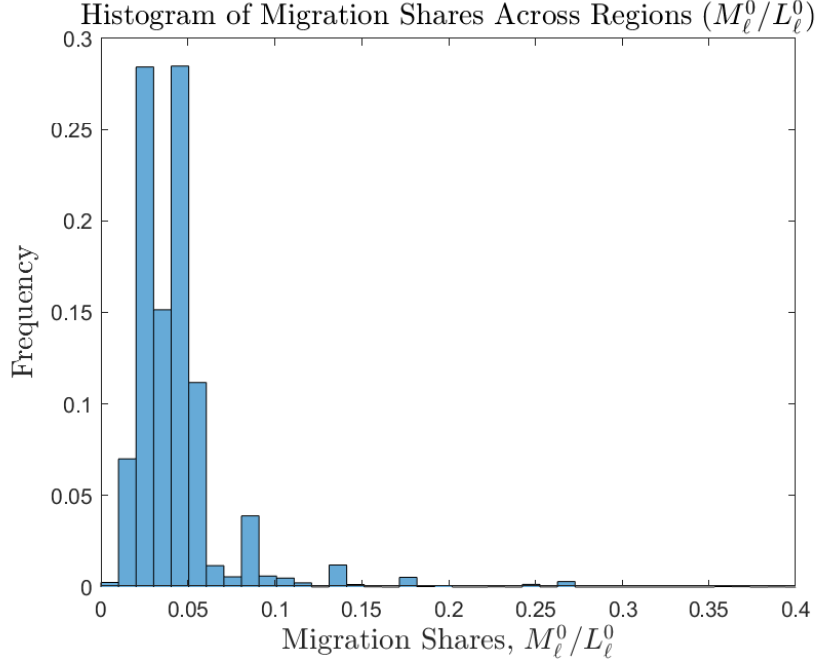
As discussed in Section 2.5, we assume that the labor market is in steady-state, so observed transitions across locations and industries reflect the relevant counterfactual transitions absent shocks. To assess the validity of this assumption in the Brazilian context, we estimate the ergodic distribution of employment across locations by computing $(\Pi^0)^\infty$ and comparing it against the observed spatial distributions of employment. We also do the same for the matrix of industry transitions.³⁶ Figure 2 shows scatter plots comparing the observed and ergodic log shares of employment at the location (panel a) and industry (panel b) levels. In both cases, the observed employment shares closely match the ergodic shares implied by the transition matrix. This similarity supports the assumption that the Brazilian labor market was close to steady state across regions and industries.

The analyses in Sections 3.3 and 4 emphasized the role of spillovers between connected locations and location-industry cells in driving migration responses to labor demand shocks. These spillovers will be particularly important in practice if these connections differ substantially for workers in different locations or industries, e.g. due to migration costs increasing in distance. To assess these differences we calculate the Herfindahl–Hirschman index (HHI) measuring the average concentration

³⁵We also find substantial heterogeneity across industries in the probability of switching industries, with rates ranging from close to zero up to 20%.

³⁶To be precise, we calculate Π^0 to the power 10,000 where Π^0 is the observed matrix of location or industry transitions. We do not repeat this analysis by location-industry cells because of the large number of small cells, for which the relative difference between the observed and ergodic sizes is noisy and uninformative.

Figure 1: Geographic Mobility Rates Across Regions



Notes: Percent of individuals migrating across locations (microregions), calculated from average yearly flows between location-industry cells in RAIS data from 1994 to 2000 as described in footnote 34. The histogram weighted by each location's initial population.

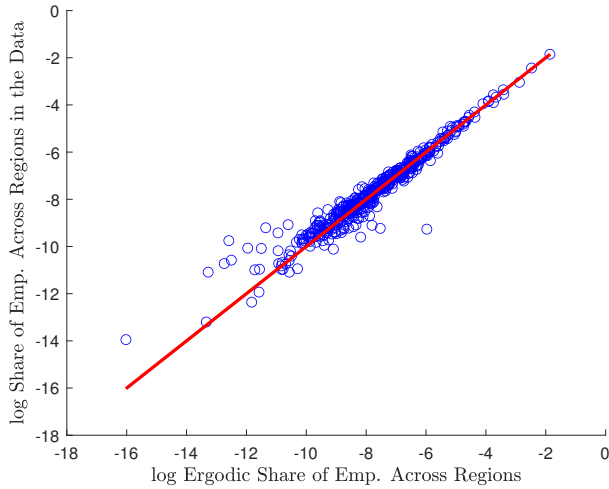
of destinations and origins among those who migrated to or from a given region:

$$HHI_\ell = \sum_{k \neq \ell} \left(\frac{\frac{1}{2} (\pi_{\ell k}^0 + \gamma_{k\ell}^0)}{1 - \frac{1}{2} (\pi_{\ell\ell}^0 + \gamma_{\ell\ell}^0)} \right)^2. \quad (34)$$

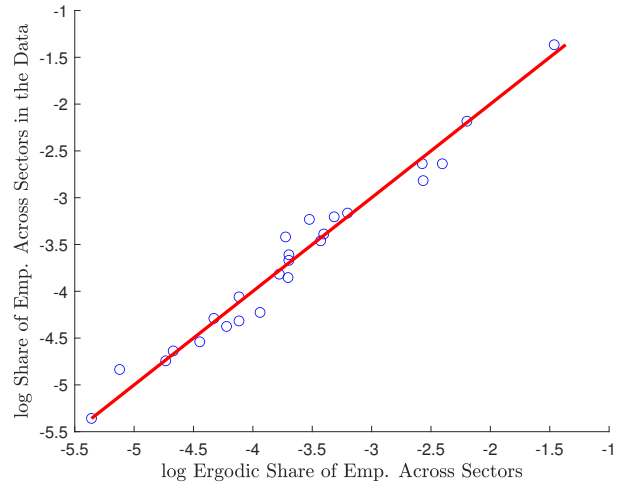
We also calculate a parallel expression for those who switched to or from industry n , HHI_n . The distributions of these concentration measures are shown in Figure 3. The average HHI_ℓ across locations is 0.165 (s.d. 0.174), which is equivalent to equally-weighted connections to only 6 other locations out of 485 possibilities. Industry transitions are more dispersed, with an average average HHI_n across industries 0.141 (s.d. 0.050), which is equivalent to equally-weighted connections to 7 other industries out of 24 possibilities. Figure 3 also makes clear that there is substantial variation in these concentration measures for both locations and industries.

Figure 2: Actual vs. Ergodic Employment Distribution

Panel (a): Across Locations



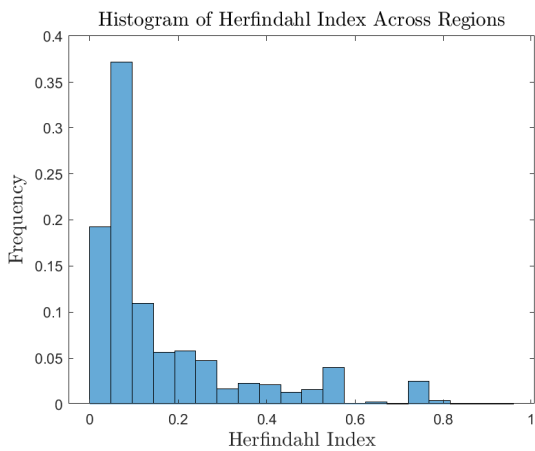
Panel (b): Across Industries



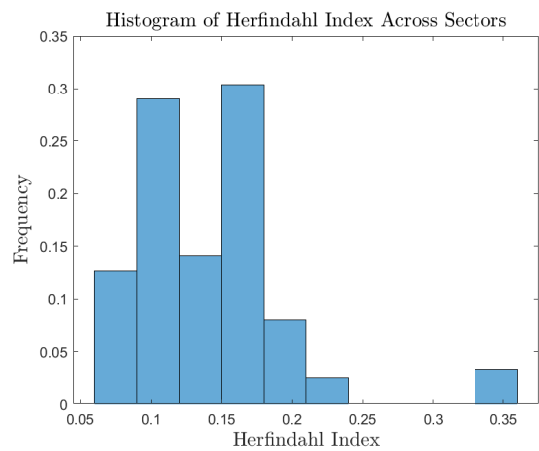
Notes: Panel (a) compares the observed log share of national employment in each location to the ergodic distribution implied by the observed transition matrix Π^0 . Panel (b) makes the same comparison across industries. 45-degree lines are shown in red. The close agreement between observed and ergodic distributions supports the steady-state assumption.

Figure 3: Concentration of Locations and Industries Among Switchers

Panel (a): Across Locations



Panel (b): Across Industries



Notes: Panel (a) shows the distribution of HHI indexes measuring the concentration of sources and destinations for those switching locations, as defined in (34), weighted by the initial regional employment. Panel (b) similarly shows the distribution of HHI indexes across industries.

6 Simulation-Based Evidence

In this section we quantitatively examine the predictive accuracy of the conventional migration regression in the context of Brazilian geography, industrial structure, and baseline migration patterns. We simulate migration behavior based on our model in response to labor demand shocks that follow a variety of different data generating processes and compare these true responses to those inferred from conventional migration regression estimates. We further compare the conventional regression with the model-based NLLS procedure.

6.1 Simulation Procedure and Calibration

To generate model-simulated migration behavior, we must first specify the distribution of labor demand shocks and calibrate the parameters θ and σ . We consider three different data generating processes for shocks. The first set of shocks are independent standard normal draws across locations, i.e. $\hat{x}_\ell \sim N(0, 1)$ and $\hat{z}_{\ell n} = \hat{x}_\ell$. We refer to these shocks as “*iid* across locations.” The second set of shocks introduces spatial correlation by assigning the same shock to all locations (microregions) in the same Brazilian state. The state-level shocks are independently and normally distributed, such that $\hat{x}_s \sim N(0, \sigma_2^2)$ and $\hat{z}_{\ell n} = \hat{x}_{s(\ell)}$, where $s(\ell)$ is the state containing location ℓ . We refer to these shocks as “*iid* across states.” Finally, we generate independently and normally distributed shocks across industries, such that $\hat{x}_n \sim N(0, \sigma_3^2)$, $\hat{z}_{\ell n} = \hat{x}_n$, and the regional shift-share measure is $\hat{z}_\ell = \sum_n \frac{L_{\ell n}^0}{L_\ell^0} \hat{x}_n$. We refer to these shocks as “*iid* across industries.” To ensure comparable magnitudes across the three types of shocks, we choose σ_2 and σ_3 so that the expected cross-location variance of shocks is equal to one.³⁷

Given the relevant vector of shocks, we generate the change in employment based on $\hat{\mathbf{L}} = \left(I - (\Psi^0)^{-1} \right) \hat{\mathbf{z}}$ (i.e. (21) without the error term, which we return to below).³⁸ Recall that Ψ^0 depends on the observed flow matrices Γ^0 and Π^0 , which we measure using the RAIS data (Section 5.1), and the parameter ratio $\frac{\theta}{\sigma}$. We draw on the literature to determine a realistic calibration of $\frac{\theta}{\sigma}$. Caliendo et al. (2019) estimate $\frac{1}{\theta} = 2.02$ across U.S. states (at the yearly level), so we set $\theta = 0.5$. In the absence of estimates of the Armington substitution elasticity across sub-national locations,

³⁷Specifically, $\sigma_2 = 1.076$ and $\sigma_3 = 5.595$ (when using flows for all workers regardless of skill).

³⁸Note that we do not impose the low-mobility assumption in the simulation, since we use (21) rather than (22). We do, however, maintain the assumption of small shocks, such that $\hat{x} \equiv dx/x = d \ln x$.

Table 2: Conventional Migration Regression Estimates – Comparison Across Models

Shocks		Model	
		Location Frictions	Location-Industry Frictions
<i>iid</i> across locations:	$100 \times \beta$	1.045	0.982
	R^2	0.577	0.608
<i>iid</i> across states:	$100 \times \beta$	0.254	0.247
	R^2	0.698	0.713
<i>iid</i> across industries:	$100 \times \beta$	0.875	0.283
	R^2	0.511	0.104

Notes: Average of regression estimates β and their associated R^2 across 500 simulations. See text for definitions of shock processes. Column “Location Frictions” simulates local employment changes using the model with cross-location frictions only (Section 2), while column “Location-Industry Frictions” simulates employment changes using the model with location-industry frictions (Section 4).

we use standard estimates of the cross-country elasticity from Broda and Weinstein (2006) and Feenstra et al. (2018), both of which find $\sigma \approx 4$. We therefore set $\frac{\theta}{\sigma} = \frac{1}{8}$ when calculating $\hat{\mathbf{L}}$. To investigate the effects of industry switching frictions, we generate versions of $\hat{\mathbf{L}}$ from both the model with regional frictions alone (Section 2) and the more general version with industry-region frictions (Section 4), with the same structural parameters.³⁹

We then estimate the conventional location-level migration regression using the model-implied employment changes and the associated regional shocks, and weighting by initial population, which yields an estimate of β and R^2 for a given simulation. We then repeat the entire process 500 times and report averages across the simulations.

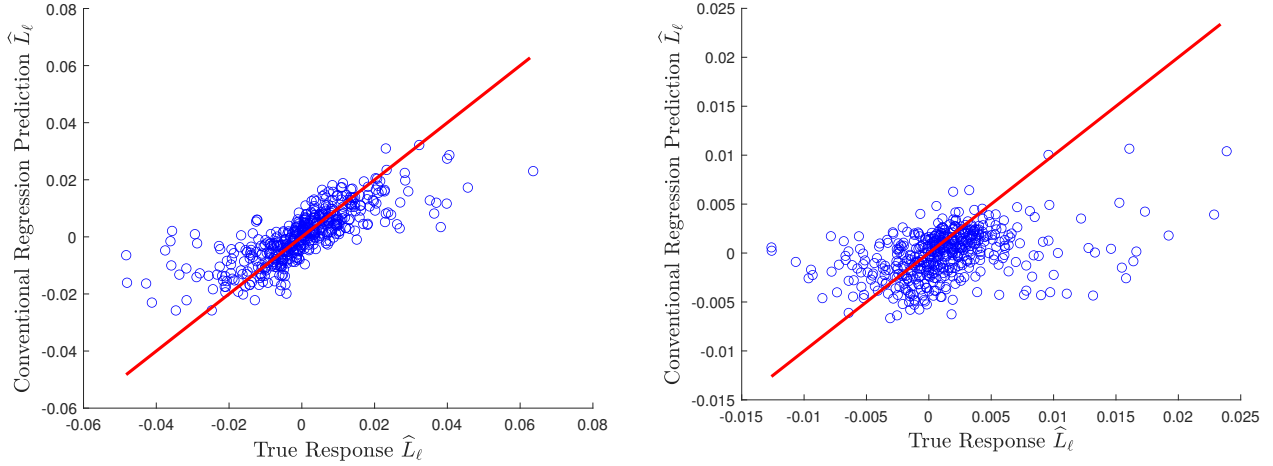
6.2 Baseline Simulation Results

Table 2 presents the baseline simulation results. To interpret the magnitudes of the estimates in the model with location frictions only, reported in the first column, we rely on the characterization of β in Theorem 1. In our calibration, $\frac{2\theta}{\sigma} = \frac{1}{4}$. Table 1 reports the average mobility rate $\frac{M^0}{L^0} = 0.042$, and the mobility rate that would prevail without mobility frictions is $\frac{\widetilde{M}^0}{L^0} \approx 1$.⁴⁰ In the first row of Table 2, when shocks are *iid* across locations, there will be no attenuation, so $\rho \approx 0$ and $\frac{1-\rho}{1-\rho} \approx 1$. Combining these, we expect $100 \times \beta \approx 1.05$, which is very similar to the realized estimate of 1.045

³⁹Artuç et al. (2010) estimate $\frac{1}{\theta} = 1.88$ across 6 U.S. industries (at the yearly level), which supports the restriction in our model with location and industry frictions that θ is common to both dimensions.

⁴⁰Footnote 18 shows that \widetilde{M}^0/L^0 equals one minus the Herfindahl index of population across regions.

Figure 4: Conventional Regression Predictions vs. True Responses for Observed Shocks
 Panel (a): *iid* shocks across locations Panel (b): *iid* shocks across industries



Notes: Scatter plots compare the predicted population response to the true model-based response for a single representative simulation of the model with location-industry frictions (Section 4). Each point represents a location. The y-axis is the predicted population response based on the conventional migration regression estimate, β . Specifically, this prediction is $\beta(\hat{z}_\ell - \bar{z})$, accounting for the intercept term in the migration regression. The x-axis is the true model-based population change in the model with location-industry frictions. The left panel shows the result for *iid* shocks across locations, and the right panel shows the result for *iid* shocks across industries. 45-degree lines are shown in red. To maintain readability, we exclude the top and bottom 1% of regions based on the true model-based population change.

in the model with only location frictions, confirming our theoretical predictions.⁴¹ The average R^2 in these simulations is only 0.577 in spite of the fact that the simulations do not include any idiosyncratic noise. This poor predictive performance reflects the fact that β omits location-specific migration intensity $\frac{M_\ell^0}{L_\ell^0}$ and predicts the spillover effects from migrant-connected locations ($\hat{z}_{-\ell} - \bar{z}$) using only the direct shock facing the location ($\hat{z}_\ell - \bar{z}$), as discussed in Section 3.3.

When we introduce spatial correlation to the shocks in the second row of Table 2, the β estimate falls sharply. The strong correlation in shocks across migrant-connected locations increases ρ and therefore decreases the attenuation factor from approximately 1 in the first row to 0.232 in the second row. Industry shift-share shocks in the third row similarly induce spatial correlation, but much less so than with state-level shocks, so the β estimate is only moderately below that for the *iid* location shocks.

While the model with location frictions alone yields a clear and intuitive decomposition of the factors driving the conventional migration regression estimate of β (equation (26)), the model

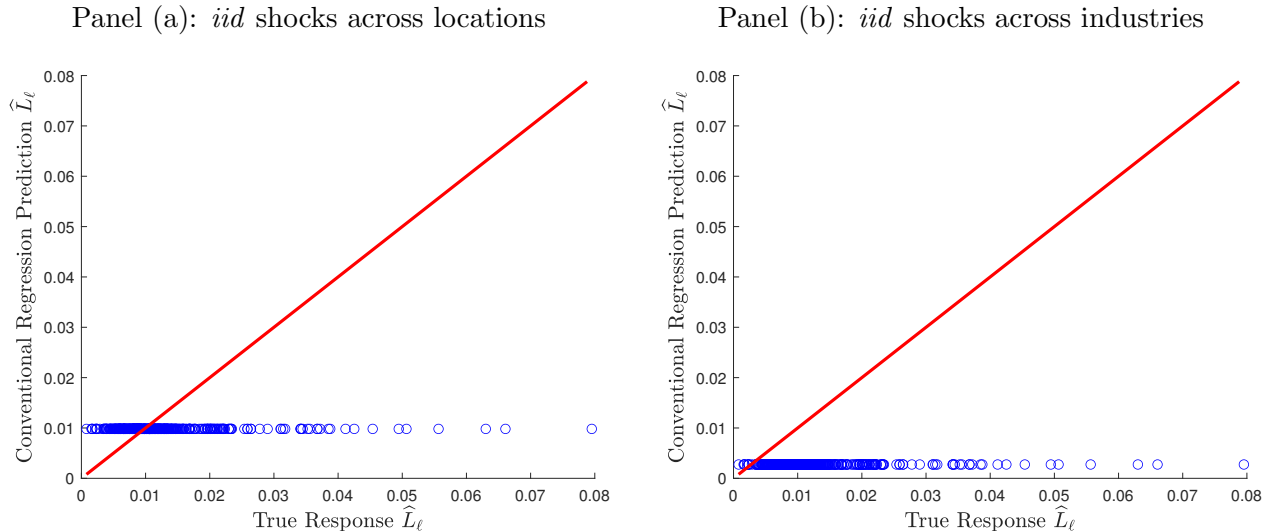
⁴¹The Table 1 coefficient could diverge from the prediction of Theorem 1 for two reasons, even with a very large number of simulation draws: the theorem uses the low-mobility approximation and characterizes the estimand of the regression, which is not the same as the estimator mean (because the ratio of expectations does not equal the expectation of the ratio in (24)). Neither of these differences turns out to be quantitatively important.

with both industry and location frictions is arguably more realistic. We present simulation results from this richer model in the second column of Table 2. When shocks are *iid* across locations, the regression estimate of 0.982 is very similar to the model with location frictions only, as is the associated R^2 . This similarity reflects the finding in (32) that the two models are identical under the low-mobility approximation. However, when we introduce industry-level shocks in the last panel, the estimate is much smaller in the model with location-industry frictions than in the model with location frictions alone. This again confirms our findings in (33) that industry frictions reduce mobility responses to industry-level shocks relative to settings with regional frictions alone. Also note that the R^2 value for industry shocks with location-industry frictions is extremely low.

Figure 4 visually presents these results, showing scatter plots comparing predicted population changes based on the conventional migration regression estimates, $\beta(\hat{z}_\ell - \bar{z})$, against the true population change based on the model with industry-region frictions for one example simulation draw. This exercise assesses the extent to which the regression is informative regarding the true effects of the observed shocks. Consistent with the R^2 values in Table 2, the regression-based predictions are quite inaccurate in many regions under both models, but the predictions are clearly substantially worse when facing industry-level shocks (in Panel (b)). The difference in x -axis scale between the two panels shows that there is less true reallocation in Panel (b), confirming the theoretical conclusion from Section 4 that industry-switching frictions reduce migration responses when labor demand shocks have an industry-specific component. In this case, the estimate of β is relatively small, so the regression predicts much less variation in population responses than the model does, and the predictions are minimally related to the true values. In this example, many regions experience substantial population changes as a result of the shocks despite the relatively small estimate of β .

Together, the results in Table 2 and Figure 4 confirm the patterns predicted in our theoretical analysis and reveal substantial quantitative attenuation when shocks are correlated across migrant-connected locations. The low R^2 values also imply that the conventional regression yields quite poor predictions of the effects of the observed shocks used to estimate β even in a setting where migration is determined by the labor demand shocks alone, without additional noise. In other words, the conventional migration regression performs poorly in generating internally valid estimates of the effects of observed shocks.

Figure 5: Conventional Regression Predictions vs. True Responses for Counterfactual Unit Shocks



Notes: Scatter plots compare the predicted population response to a counterfactual unit shock to a single location against the true model-based response for a single representative simulation. Each point represents a location. The y-axis is the predicted population response based on the conventional migration regression estimate, β . The x-axis is the true model-based population change in the model with location-industry frictions (Section 4) when the relevant location faces a unit shock. The left panel shows the result when β is estimated using iid shocks across locations, and the right panel shows the result when β is estimated using iid shocks across industries. 45-degree lines are shown in red.

Now consider interpreting the estimate of β as the effect of a counterfactual unit labor demand shock to a single location on that location’s population. The regression-based prediction for this counterfactual is $\beta \times 1$, so the counterfactual prediction is the constant β for all locations. We calculate the true model-based population change when individually shocking each location and plot the responses against the estimate of β in Figure 5. Panel (a) considers the average β estimate using *iid* regional shocks in the model with location-industry frictions, where $100 \times \beta = 0.982$ (see Table 2). While the regression estimate based on *iid* regional shocks matches the mean response, it omits significant heterogeneity in the magnitude of the true counterfactual responses in each location. The situation is even worse when β is estimated using a regional shift-share measure based on *iid* industry shocks in Panel (b), where $100 \times \beta = 0.283$. Not only does the estimate omit all heterogeneity, but it is subject to substantial attenuation due to the shock correlation across locations and the industry-switching frictions. In this case, the regression-based counterfactual estimate substantially understates the true effect in nearly every location.

Table 3: Conventional Migration Regression Estimates – Comparison Across Skill Levels with Location-Industry Frictions

Shocks		All Workers	High-Skilled	Low-Skilled
<i>iid</i> across locations:	$100 \times \beta$	0.982	1.014	0.956
	R^2	0.608	0.539	0.619
<i>iid</i> across states:	$100 \times \beta$	0.247	0.285	0.226
	R^2	0.713	0.703	0.669
<i>iid</i> across industries:	$100 \times \beta$	0.283	0.560	0.234
	R^2	0.104	0.139	0.110

Notes: Average of regression estimates β and R^2 across 500 simulations. See text for details of shock processes. All simulations are based on the model with location-industry frictions (Section 4). High-skilled workers are those with at least a high-school degree, and Low-skilled workers are those with less than a high-school degree.

6.3 Simulations by Skill Level

The simulation results thus far make clear that estimates from the conventional migration regression do not accurately reflect the effects of historical shocks on affected locations, nor can they be interpreted as the effect of counterfactual shocks to individual locations. We now investigate conventional migration estimates separately by skill level. Prior work has emphasized that less skilled workers’ location choices are less responsive to local labor demand shocks than those of more highly skilled workers (Bound and Holzer, 2000; Cadena and Kovak, 2016). Our goal is to understand the extent to which the various problems identified above may explain these commonly-observed differences. For example, if labor demand shocks facing less skilled workers were more correlated between migrant-connected locations, their β estimates would be more attenuated than those for more skilled workers even if both groups of workers had similar mobility parameters.

To investigate this possibility, we implement the simulation procedure described in the preceding subsection separately for high-skilled and low-skilled workers.⁴² We assign the same value of $\frac{\theta}{\sigma} = \frac{1}{8}$ to both education groups so that both groups would be equally responsive to shocks to one region at a time, given that their average mobility rates are also similar (as shown by Table 1). The identical mobility parameters and similar average mobility between the two groups implies that any substantial differences in conventional migration regression estimates across the two groups can only be explained by differences shock correlation or differences in the distribution of shocks faced by each group.

⁴²Specifically, we construct the mobility flows across locations and regions by skill level separately and redo the entire analysis. We do not consider a model in which both skill groups interact in the economy.

Table 3 shows the conventional migration estimates for all workers (replicating the last column of Table 2) and then by education group for the three different shock processes in the model with location-industry frictions. The β estimates are quite similar across skill groups when shocks are *iid* across locations, reflecting our imposition of the same structural parameters on both groups and the groups' similar average migration rates. Both groups also experience roughly similar attenuation of β when facing spatially correlated state-level shocks. However, the two groups exhibit very different estimates when facing *iid* shocks across industries. The β estimate for low-skilled workers is less than half the magnitude of that for high-skilled workers. This difference suggests that low-skilled workers may appear to respond less to local industry shift-share shocks not because of fundamental differences in regional mobility but because they face different shift-share shocks or because they have larger costs of switching industries than high-skilled workers. These distinctions are essential for determining what kinds of policies will be most effective at addressing regional disparities in unemployment among low-skilled workers.

6.4 Introducing Noise

The preceding simulations determine the true population changes based on the model's structure and simulated labor demand shocks alone. In that setting, the model fits the data perfectly by construction, so we were unable to assess the quality of estimates based on the proposed NLLS procedure introduced in Section 3.4. Here, we add noise from unobserved changes in labor demand or supply (assumed orthogonal to the observed labor demand shocks to avoid introducing endogeneity bias), to assess the relative performance of the conventional migration regression and the proposed NLLS procedure and to better mimic the data observed in a typical study of migration responses to local shocks.

Specifically, for a shock vector $\hat{\mathbf{z}}$, we calculate the change in population as $\hat{\mathbf{L}} = \hat{\mathbf{L}}^{\text{due to } \hat{\mathbf{z}}} + \zeta$ where $\hat{\mathbf{L}}^{\text{due to } \hat{\mathbf{z}}} = \left(I - (\Psi^0)^{-1} \right) \hat{\mathbf{z}}$ and Ψ^0 is computed using the true parameter $\frac{\theta}{\sigma} = \frac{1}{8}$. We focus on the model with location-industry frictions, so each element of the vectors in this expression is a location-industry combination. We allow the unobserved shocks in $\zeta_{\ell n}$ to consist of additive location, industry, and location-industry components, such that

$$\zeta_{\ell n} = \epsilon_{\ell} + \epsilon_n + \epsilon_{\ell n}.$$

To ensure a realistic scale for this noise term, we take the observed changes in employment in each location-industry cell and regress them on location fixed effects and industry fixed effects, which allows us to measure the location-level variation, industry-level variation, and residual location-industry variation, which we use to calibrate the variance of each noise component.⁴³

We compare the in-sample fit of four methods for estimating the population effects of the simulated labor demand shocks. We first estimate β from the conventional regression (23) and, like before, take $\beta(\hat{z}_\ell - \bar{z})$ as the predicted population growth in location ℓ . We then estimate θ/σ with two versions of the NLLS specification (29) based on the correctly specified model, which allows for location-industry mobility frictions. First, we perform the estimation on location-industry observations, with the simulated $\hat{L}_{\ell n}$ as the dependent variable and the model's prediction for it as a function of $\hat{\mathbf{z}}$ and θ/σ on the right-hand side. The second version is analogous, except estimation is done with regional observations, in parallel to the conventional regression. That is, we use the simulated \hat{L}_ℓ as the dependent variable and the model's prediction for it, which aggregates predicted $\hat{L}_{\ell n}$ across industries for each region, on the right-hand side. Since both of these approaches are based on the correctly specified model, their prediction is only imperfect because of the noisy estimates of θ/σ . Finally, we consider NLLS estimation of (29) where $\Psi^0(\theta/\sigma)$ is constructed from the misspecified baseline model that does not allow industry mobility frictions, and again using \hat{L}_ℓ as the dependent variable. The advantage of this specification is that it is feasible without data on mobility across location-industry cells; it only requires regional flows, which are much more readily available in many countries.

We use the Root Mean Square Error (RMSE) as the measure of in-sample predictive quality for regional population changes \hat{L}_ℓ . Specifically, given predictions $\hat{\mathbf{L}}_{\ell;s}^{\text{predicted}}$ from one of the four methods in simulation s , we compute

$$RMSE = \sqrt{\frac{1}{S} \sum_{s=1}^S \left[\sum_{\ell=1}^L \frac{L_\ell^0}{L^0} \left(\hat{L}_{\ell;s}^{\text{due to } \hat{\mathbf{z}}} - \hat{L}_{\ell;s}^{\text{predicted}} \right)^2 \right]}, \quad (35)$$

which averages squared prediction errors both across locations (with population weights) and across

⁴³From historical data, we estimate $\hat{L}_{\ell n} = \nu_\ell + \nu_n + \varepsilon_{\ell n}$, where ν_ℓ are location fixed effects, ν_n are industry fixed effects, and $\varepsilon_{\ell n}$ is the error. The employment-weighted standard deviation of the estimated location terms is 0.0158, of the estimate industry terms is 0.0139, and of the estimated residual is 0.0512. We then simulate normally-distributed noise components as $\varepsilon_\ell \sim \mathcal{N}(0, 0.0158^2)$, $\varepsilon_n \sim \mathcal{N}(0, 0.0139^2)$, and $\varepsilon_{\ell n} \sim \mathcal{N}(0, 0.0512^2)$. Finally, we demean the resulting overall noise term $\zeta_{\ell n}$ so $\sum_{\ell,n} \frac{L_{\ell n}^0}{L^0} \zeta_{\ell n} = 0$.

Table 4: RMSE of Conventional Regression and NLLS Predictions

Prediction method	RMSE, relative to uninformative prediction	
	<i>iid</i> location shocks	<i>iid</i> industry shocks
Conventional regression	0.719	1.020
NLLS, region-industry level	0.171	0.029
NLLS, regional level	0.250	0.339
NLLS, misspecified regional model	0.262	0.917

Notes: Each row corresponds to a method of predicting the effect of observed shocks on regional population, while each column defines the shock process; see the text for details. Each cell reports the ratio of the root mean squared error (RMSE) for a given prediction method to the RMSE from the uninformative prediction, computed via (35) and (36), respectively. All simulations are based on the model with location-industry frictions (Section 4).

$S = 500$ simulations. We rescale this RMSE measure relative to its value for the uninformed prediction, $\hat{L}_{\ell;s}^{\text{predicted}} = 0$, i.e. by the square root of the average cross-simulation variance of the component of population changes due to the shock:

$$RMSE_{\text{uninformative}} = \sqrt{\frac{1}{S} \sum_{s=1}^S \left[\sum_{\ell=1}^L \frac{L_{\ell}^0}{L^0} \left(\hat{L}_{\ell;s}^{\text{due to } \mathbf{z}} \right)^2 \right]}. \quad (36)$$

Table 4 reports the results for our four methods and for *iid* location and *iid* industry shock processes. The first row confirms that predictions by the conventional regression are very poor: it outperforms the uninformative prediction by less than 30% when the shocks are location-specific and performs 2% *worse* than the uninformative prediction for industry shocks. The second and third rows show that NLLS performs well when taking into account mobility frictions across both regions and industries. When estimated at the location-industry level, its RMSE is only 17% of that of the uninformative prediction with *iid* location shocks, and as little as 3% for *iid* industry shocks. For *iid* location shocks, estimation at the more aggregated regional level increases the estimation error only slightly, from 17% to 25% of the uninformative prediction RMSE. However, for *iid* industry shocks, data aggregation raises the RMSE from 3% to 34% — although still three times lower than with the conventional regression.⁴⁴ Finally, the fourth row of Table 4 reports the predictive quality of the misspecified model without industry frictions. For location shocks, the

⁴⁴This gap in performance can be linked to how much of the variation of the regional vs. region-industry levels the observed shocks capture. With *iid* industry shocks, 83.1% of the $\hat{L}_{\ell n}$ variation is due to the observed shocks, compared to only 10.0% for \hat{L}_{ℓ} (measured by the employment-weighted R^2 on average across simulations). This difference is much smaller, and in the opposite direction, for *iid* regional shocks: they on average explain 7.7% of the variation in $\hat{L}_{\ell n}$ but a higher 21.2% of the variation in \hat{L}_{ℓ} .

RMSE is almost identical to the previous row, at 26%. Indeed, as discussed before, the predictions of the benchmark and full models would be identical if the low-mobility approximation was precise. However, with *iid* industry shocks the misspecified model provides very poor predictions, with a RMSE of 92% relative to the uninformative prediction and only slightly ahead of the conventional regression.

The absolute and, possibly, relative performance of different methods may depend on how much useful variation the observed shocks provide relative to the noise in the data — a parameter which may vary across empirical settings. To check robustness of our findings, we therefore repeat the Table 4 analysis varying the relative variance of $\hat{\mathbf{z}}$ and ζ , specifically by multiplying ζ by a factor $\delta \in [0, 4]$, with $\delta = 1$ corresponding to the Table 4 results. Appendix Figure A1 shows that the results are robust.⁴⁵

Taken together, these results yield two lessons. First, accounting for the spillovers via the model-consistent NLLS procedure allows one to capture the population responses of local labor demand shocks even in the presence of noise in the data, which the conventional regression is not capable of. Second, ignoring the industry dimension of the data — in either the unit of observations or the model employed — is relatively innocuous when the shocks are purely region-specific. However, when the shocks are industry-driven, it is crucial to take the structure of industry mobility into account, in using the appropriate model as well as estimating the structural parameter at the disaggregated location-industry level.

7 Conclusion

This paper has examined how to interpret conventional migration regression estimates relating changes in local population or employment to observed local labor demand shocks. Using a simple model of local labor markets with mobility costs, we find that common conclusions drawn from migration regression estimates are likely to be substantially misleading. Analytical results and quantitative simulations show that conventional migration regression estimates provide inaccurate estimates of the within-sample effects of observed shocks on local populations and are uninformative

⁴⁵The only exception is NLLS estimated from *iid* industry shocks at the level of regions, which is sensitive to δ : it performs well for small δ (although uniformly worse than NLLS estimation by region-industry) but not for large amounts of noise.

regarding the effects of counterfactual shocks to one or many locations.

Conventional migration regression estimates are therefore not informative regarding the magnitude of migration frictions or the potential benefits of policies aimed at helping workers relocate to stronger labor markets. Nor should the estimates be used to justify omitting inter-regional migration from quantitative economic models of local labor markets. Instead, researchers should adopt methods accounting for spillovers of shocks between connected locations, as in our proposed NLS procedure. Yet, to implement that and related analyses, the data demands are significant. Our analysis using Brazilian data shows the substantial practical benefit of observing transitions between relatively detailed location-industry cells to successfully capture the interrelationships in a large and diverse economy.

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A Theory Appendix

A.1 Incorporating Labor Supply Shocks

In this appendix we show that the expressions from Section 2 extend naturally when the moving costs $\tau_{\ell d}$, in addition to D_ℓ , are allowed to change, generating local labor supply shocks. In that case, (12) is replaced by

$$\begin{aligned}\hat{L}_d &= \sum_{\ell} \gamma_{\ell d} \hat{\pi}_{\ell d} \\ &= \theta \left(\hat{w}_d - \sum_{\ell} \gamma_{\ell d} \sum_{d'} \pi_{\ell d'} \hat{w}_{d'} \right) + \nu_d\end{aligned}$$

where the labor supply shock is defined as

$$\nu_d = -\theta \sum_{\ell} \gamma_{\ell d} \left(\hat{\tau}_{\ell d} - \sum_{d'} \pi_{\ell d'} \hat{\tau}_{\ell d'} \right).$$

The supply shock is high when moving costs to d decline, relative to the moving costs from the same origins to other destinations. In vector form, $\hat{\mathbf{L}} = \theta (I - \Gamma' \Pi) \hat{\mathbf{w}} + \boldsymbol{\nu}$ with $\boldsymbol{\nu} = \{\nu_d\}$. Solving the system of demand and supply (i.e. using (9)), this implies

$$\hat{\mathbf{L}} = (I - \Psi^{-1}) \hat{\mathbf{D}} + \Psi^{-1} \boldsymbol{\nu}.$$

Finally, after the steady state, (19) yields

$$\hat{\mathbf{L}} = \left(I - (\Psi^0)^{-1} \right) \hat{\mathbf{z}} + \zeta_2 + (\Psi^0)^{-1} \boldsymbol{\nu},$$

which generates a second, supply-driven, error term. The results of the paper apply if the $\hat{\mathbf{z}}$ shocks are mean-independent from both unobserved labor demand and labor supply shocks.

A.2 Low-Mobility Approximation Derivation

Plugging $\Gamma = I + \Delta\Gamma$ and $\Pi = I + \Delta\Pi$ into (16) and assuming $\Delta\Gamma' \Delta\Pi \approx 0$ yields

$$\Psi \approx I - \frac{\theta}{\sigma} (\Delta\Gamma' + \Delta\Pi).$$

We next must find Ψ^{-1} . Let $A \equiv \frac{\theta}{\sigma} (\Delta\Gamma' + \Delta\Pi)$ such that $\Psi \approx I - A$. Then define the infinite series $S \equiv I - A + A^2 - A^3 \dots$. Under the low-mobility assumption, $\Psi \approx S$ since $\Delta\Gamma' \Delta\Pi \approx \Delta\Gamma' \Delta\Gamma' \approx \Delta\Pi \Delta\Pi \approx \mathbf{0}$. Since $S + SA = S(I + A) = I$, we have $S^{-1} = I + A$ and in turn $\Psi^{-1} \approx I + A$, which is equivalent to

$$\Psi^{-1} \approx I + \frac{\theta}{\sigma} (\Delta\Gamma' + \Delta\Pi).$$

Plugging this into (14) and simplifying yields

$$\hat{\mathbf{L}} = \frac{\theta}{\sigma} (I - \Gamma' + I - \Pi) \hat{\mathbf{D}},$$

which is (17) in matrix notation.

A.3 $\hat{\beta}$ Is Close to β in Large Samples

In this appendix we provide the regularity conditions under which both $\hat{\beta}$ and β converge to the same number in an asymptotic sequence of economies with a growing number of domestic regions, $r = |\mathcal{L}|$. Under those conditions $\hat{\beta}$ and β are expected to be similar to each other when the observed number of regions is large.

We consider a general sequence of data-generating processes, indexed by r , which jointly determine all relevant economic variables. We have:

Proposition 2. *Suppose $\sum_{\ell} \frac{L_{\ell}^0}{L^0} \hat{L}_{\ell} (\hat{z}_{\ell} - \bar{z}) \xrightarrow{p} C$ and $\sum_{\ell} \frac{L_{\ell}^0}{L^0} (\hat{z}_{\ell} - \bar{z})^2 \xrightarrow{p} V > 0$ as $r \rightarrow \infty$, and both sequences are uniformly integrable. Then $\hat{\beta} \xrightarrow{p} \frac{C}{V}$ and $\beta \rightarrow \frac{C}{V}$.*

Proof. The first statement follows by the continuous mapping theorem. For the second statement, note that uniform integrability implies $\mathbb{E} \left[\sum_{\ell} \frac{L_{\ell}^0}{L^0} \hat{L}_{\ell} (\hat{z}_{\ell} - \bar{z}) \right] \rightarrow C$ and $\mathbb{E} \left[\sum_{\ell} \frac{L_{\ell}^0}{L^0} (\hat{z}_{\ell} - \bar{z})^2 \right] \rightarrow V$. Thus, $\hat{\beta} \rightarrow \frac{C}{V}$, as required. \square

A.4 Proof of Theorem 1

We prove a generalization of Theorem 1 which does not require homoskedasticity of shocks:

$$\beta = \frac{2\theta}{\sigma} \cdot \frac{\sum_{\ell} v_{\ell} M_{\ell}^0 (1 - \beta_{\ell})}{\sum_{\ell} v_{\ell} \tilde{M}_{\ell}^0 (1 - \tilde{\beta}_{\ell})}, \quad (37)$$

where $v_{\ell} = \text{Var} [\hat{z}_{\ell}]$, $\beta_{\ell} = \text{Cov} [\hat{z}_{-\ell}, \hat{z}_{\ell}] / v_{\ell}$, $\tilde{\beta}_{\ell} = \text{Cov} [\tilde{z}_{-\ell}, \hat{z}_{\ell}] / v_{\ell}$, and $\tilde{z}_{-\ell} = \sum_{d \neq \ell} \frac{(\tilde{M}_{d}^0 + \tilde{M}_{d\ell}^0)/2}{\tilde{M}_{\ell}^0} \hat{z}_d$. At the end of this section we show that (37) implies the Theorem 1 statement under homoskedasticity. Given that regression (23) includes the constant and our interest is in the slope parameter, we assume without loss of generality that the shocks have zero expectation, $\mu = 0$.

We start with the numerator of β , which can be represented as

$$\begin{aligned} \mathbb{E} \left[\sum_{\ell} L_{\ell}^0 \hat{L}_{\ell} (\hat{z}_{\ell} - \bar{z}) \right] &= \mathbb{E} \left[\sum_{\ell} L_{\ell}^0 \hat{L}_{\ell} \hat{z}_{\ell} \right] \\ &= \mathbb{E} \left[\frac{2\theta}{\sigma} \sum_{\ell} M_{\ell}^0 \hat{z}_{\ell} (\hat{z}_{\ell} - \hat{z}_{-\ell}) \right] \\ &= \frac{2\theta}{\sigma} \sum_{\ell} M_{\ell}^0 v_{\ell} (1 - \beta_{\ell}). \end{aligned} \quad (38)$$

Here the first line used the fact that $\sum_{\ell} L_{\ell}^0 \hat{L}_{\ell} \bar{z} = \bar{z} \sum_{\ell} L_{\ell}^0 \hat{L}_{\ell} = \bar{z} \hat{L} = 0$ because total national population is not allowed to change in the model. The second line plugged in (22), and the last line used the definitions of v_{ℓ} and β_{ℓ} .

Now turn to the denominator of β . Since \bar{z} is a weighted average of the shock to ℓ and other regions, specifically $\bar{z} = \frac{L_{\ell}^0}{L^0} \hat{z}_{\ell} + \left(1 - \frac{L_{\ell}^0}{L^0}\right) \tilde{z}_{-\ell}$, we have

$$\hat{z}_{\ell} - \bar{z} = \left(1 - \frac{L_{\ell}^0}{L^0}\right) (\hat{z}_{\ell} - \tilde{z}_{-\ell}). \quad (39)$$

Thus,

$$\begin{aligned}
\mathbb{E} \left[\sum_{\ell} L_{\ell}^0 (\hat{z}_{\ell} - \bar{z})^2 \right] &= \mathbb{E} \left[\sum_{\ell} L_{\ell}^0 \hat{z}_{\ell} (\hat{z}_{\ell} - \bar{z}) \right] \\
&= \mathbb{E} \left[\sum_{\ell} L_{\ell}^0 \left(1 - \frac{L_{\ell}^0}{L^0} \right) \hat{z}_{\ell} (\hat{z}_{\ell} - \tilde{z}_{-\ell}) \right] \\
&= \mathbb{E} \left[\sum_{\ell} \widetilde{M}_{\ell}^0 \hat{z}_{\ell} (\hat{z}_{\ell} - \tilde{z}_{-\ell}) \right] \\
&= \sum_{\ell} \widetilde{M}_{\ell}^0 v_{\ell} (1 - \tilde{\beta}_{\ell}). \tag{40}
\end{aligned}$$

Here the first line used $\sum_{\ell} L_{\ell}^0 \bar{z} (\hat{z}_{\ell} - \bar{z}) = \bar{z} \sum_{\ell} L_{\ell}^0 (\hat{z}_{\ell} - \bar{z}) = 0$ by definition of \bar{z} . The second line used (39). The third line used the definition of \widetilde{M}_{ℓ}^0 , and the final line used the definition of $\tilde{\beta}_{\ell}$. Combining (38) and (40) directly yields (37).

Finally, suppose shocks are homoskedastic. Then, the numerator of β equals

$$\begin{aligned}
\frac{2\theta}{\sigma} \sum_{\ell} M_{\ell}^0 v_{\ell} (1 - \beta_{\ell}) &= \frac{2\theta}{\sigma} \sum_{\ell} \left(M_{\ell}^0 v - \sum_{k \neq \ell} \frac{M_{k\ell}^0 + M_{\ell k}^0}{2} \text{Cov} [\hat{z}_k, \hat{z}_{\ell}] \right) \\
&= \frac{2\theta}{\sigma} v \sum_{\ell} \left(M_{\ell}^0 - \sum_{k \neq \ell} \frac{M_{k\ell}^0 + M_{\ell k}^0}{2} \frac{\text{Cov} [\hat{z}_k, \hat{z}_{\ell}]}{v} \right) \\
&= \frac{2\theta}{\sigma} v M^0 \left(1 - \sum_{k \neq \ell} \frac{M_{k\ell}^0 + M_{\ell k}^0}{2} \text{Corr} [\hat{z}_k, \hat{z}_{\ell}] \right) \\
&= \frac{2\theta}{\sigma} v M^0 (1 - \rho).
\end{aligned}$$

The denominator of β analogously equals $v \widetilde{M}^0 (1 - \tilde{\rho})$, and the statement of Theorem 1 follows.

A.5 Proof $\beta(\hat{z}_{\ell} - \bar{z})$ Yields MSE-Minimizing Predicted Population Growth

Proposition. $\beta(z_{\ell} - \bar{z})$ is the best linear predictor of \hat{L}_{ℓ} among all $b(z_{\ell} - \bar{z})$, i.e. after demeaning the shocks, in the sense that it solves

$$\min_b \mathbb{E} \left[\sum_{\ell} L_{\ell} \left(\hat{L}_{\ell} - b(z_{\ell} - \bar{z}) \right)^2 \right]. \tag{41}$$

Proof. The first order condition for (41) yields

$$\begin{aligned}
\mathbb{E} \left[\sum_{\ell} L_{\ell} \left(\hat{L}_{\ell} - b(z_{\ell} - \bar{z}) \right) \cdot (z_{\ell} - \bar{z}) \right] &= 0 \\
\mathbb{E} \left[\sum_{\ell} L_{\ell} \hat{L}_{\ell} (z_{\ell} - \bar{z}) \right] &= b \cdot \mathbb{E} \left[\sum_{\ell} L_{\ell} (z_{\ell} - \bar{z})^2 \right],
\end{aligned}$$

which implies $b = \beta$. □

A.6 Relationship Between $\beta \approx 0$ and Local Economic Outcomes

In this appendix we show in the context of our baseline model of Section 2 that the regression of local wage changes on the \hat{z} shock is approximately unbiased if and only if β from the migration regression is small, regardless of the reason why that it is small.⁴⁶

By (8) and (19),

$$\hat{w}_\ell = \frac{1}{\sigma} \left(\hat{D}_\ell - \hat{L}_\ell \right) = \frac{1}{\sigma} \left(\hat{z}_\ell + \zeta_{1\ell} - \hat{L}_\ell \right).$$

Therefore, a conventional regression of \hat{w}_ℓ on the regional shock \hat{z}_ℓ would produce an estimand $\frac{1}{\sigma}(1 - \beta)$. This estimand is close to $\frac{1}{\sigma}$ whenever $\beta \approx 0$, regardless of the causes, described in Theorem 1. Note, however, that in some locations fitted values from the wage regression, $\frac{1}{\sigma}(1 - \beta)\hat{z}_\ell$, may be far from the true effect, $\frac{1}{\sigma}(\hat{z}_\ell - \hat{L}_\ell)$, because migration responses \hat{L}_ℓ can be large in some regions. Moreover, the regression-based predicted effect of a counterfactual shock to a specific location ℓ , $\frac{1}{\sigma}(1 - \beta)$, may differ substantially from the true effect of $\frac{1}{\sigma} \left(1 - \frac{2\theta}{\sigma} \frac{M_\ell^0}{L_\ell^0} \right)$, for locations with high steady-state migration shares.

A.7 Invariance to Recentering

In this appendix we show that recentering as in Borusyak and Hull (2021) is not needed for the NLLS problem (30) when the shocks are unconditionally as-good-as-randomly assigned to all regions, and how it can be performed with conditional as-good-as-random assignment.

Denote $\tilde{\Psi}^0(\lambda) = I - \Psi^0(\lambda)^{-1}$ and let $\tilde{\Psi}_\ell^0(\lambda)$ be the ℓ 's row of $\tilde{\Psi}^0(\lambda)$, such that $\hat{L} = \tilde{\Psi}^0 \left(\frac{\theta}{\sigma} \right) \hat{z} + \zeta_2$ and $\hat{L}_\ell = \tilde{\Psi}_\ell^0(\lambda) \hat{z} + \zeta_{2\ell}$. As we have shown in footnote 12, $\tilde{\Psi}^0(\lambda)\iota = 0$ (for any λ), and thus $\frac{\partial \tilde{\Psi}^0}{\partial \lambda} \iota = 0$ as well, where $\frac{\partial \tilde{\Psi}^0}{\partial \lambda}$ is a matrix of element-by-element derivatives of $\tilde{\Psi}^0(\lambda)$.

The first order condition corresponding to the NLLS problem (30) is

$$\mathbb{E} \left[\sum_\ell \left(\hat{L}_\ell - \tilde{\Psi}_\ell^0(\lambda) \hat{z} \right) \cdot \frac{\partial \tilde{\Psi}_\ell^0}{\partial \lambda} \hat{z} \right] = 0. \quad (42)$$

It holds at the true $\lambda = \frac{\theta}{\sigma}$ if and only if

$$\mathbb{E} \left[\sum_\ell \zeta_{2\ell} \cdot \frac{\partial \tilde{\Psi}_\ell^0}{\partial \lambda} \hat{z} \right] = 0.$$

When $\mathbb{E}[\hat{z}_\ell | \zeta_2] = \mu$ for all ℓ , i.e. in the unconditional as-good-as-random assignment case, this holds because, by the law of iterated expectations,

$$\mathbb{E} \left[\sum_\ell \zeta_{2\ell} \cdot \frac{\partial \tilde{\Psi}_\ell^0}{\partial \lambda} \hat{z} \right] = \mathbb{E} \left[\sum_\ell \zeta_{2\ell} \cdot \frac{\partial \tilde{\Psi}_\ell^0}{\partial \lambda} \mu \right] = 0.$$

This situation contrast with conditionally as-good-as-random shocks, formalized by $\mathbb{E}[\hat{z}_\ell | \zeta_2] = \tilde{\mu}' q_\ell$, where q_ℓ is a vector of observables. This weaker assumption is appropriate, for instance,

⁴⁶In a model extension (available by request) which allows for the choice of non-employment we establish a similar result for regressions in which the outcome variable is local employment change, which is now distinct from the change in local population.

when \hat{z}_ℓ is a shift-share variable based on some shifters (e.g. the growth of import penetration from China) which only happen in manufacturing industries, with q_ℓ including the regional share of manufacturing employment in addition to the intercept (Borusyak et al., 2022). In that case the NLLS moment condition (42) need not hold, and its recentered version should be used (Borusyak and Hull, 2021):

$$\mathbb{E} \left[\sum_{\ell} \left(\hat{L}_\ell - \tilde{\Psi}_\ell^0(\lambda) \hat{\mathbf{z}} \right) \cdot \frac{\partial \tilde{\Psi}_\ell^0}{\partial \lambda} (\hat{\mathbf{z}} - Q\tilde{\mu}) \right] = 0,$$

where Q collects the q_ℓ , and $\tilde{\mu}$ is estimated in a zeroth step.

A.8 Non-Linear Least Squares Identification

In this appendix we prove that $\frac{\theta}{\sigma}$ uniquely solves the minimization problem (30) whenever the variance-covariance matrix of $\hat{\mathbf{z}}$ is non-degenerate (i.e., positive definite).

Denoting $\tilde{\Psi}^0(\lambda) = I - \Psi^0(\lambda)^{-1}$, we have $\hat{\mathbf{L}} = \tilde{\Psi}^0\left(\frac{\theta}{\sigma}\right) \hat{\mathbf{z}} + \zeta_2$. Thus, the NLLS objective function (in expectation) can be written as

$$\begin{aligned} & \mathbb{E} \left[\left(\hat{\mathbf{L}} - \tilde{\Psi}^0(\lambda) \hat{\mathbf{z}} \right)' \left(\hat{\mathbf{L}} - \tilde{\Psi}^0(\lambda) \hat{\mathbf{z}} \right) \right] \\ &= \mathbb{E} \left[\left(\tilde{\Psi}^0\left(\frac{\theta}{\sigma}\right) \hat{\mathbf{z}} - \tilde{\Psi}^0(\lambda) \hat{\mathbf{z}} + \zeta_2 \right)' \left(\tilde{\Psi}^0\left(\frac{\theta}{\sigma}\right) \hat{\mathbf{z}} - \tilde{\Psi}^0(\lambda) \hat{\mathbf{z}} + \zeta_2 \right) \right] \\ &= \mathbb{E} \left[\left(\tilde{\Psi}^0\left(\frac{\theta}{\sigma}\right) (\hat{\mathbf{z}} - \mu\iota) - \tilde{\Psi}^0(\lambda) (\hat{\mathbf{z}} - \mu\iota) + \zeta_2 \right)' \left(\tilde{\Psi}^0\left(\frac{\theta}{\sigma}\right) (\hat{\mathbf{z}} - \mu\iota) - \tilde{\Psi}^0(\lambda) (\hat{\mathbf{z}} - \mu\iota) + \zeta_2 \right) \right] \\ &= \text{Var} \left[\left(\tilde{\Psi}^0\left(\frac{\theta}{\sigma}\right) - \tilde{\Psi}^0(\lambda) \right) \hat{\mathbf{z}} \right] + \mathbb{E} [\zeta_2' \zeta_2], \quad (43) \end{aligned}$$

where the third line uses $\tilde{\Psi}^0(\lambda)\iota = 0$ (see footnote 12 and Appendix A.7) and the last line follows since, under $\mathbb{E}[\hat{\mathbf{z}} - \mu\iota \mid \zeta_2] = 0$, the cross-terms

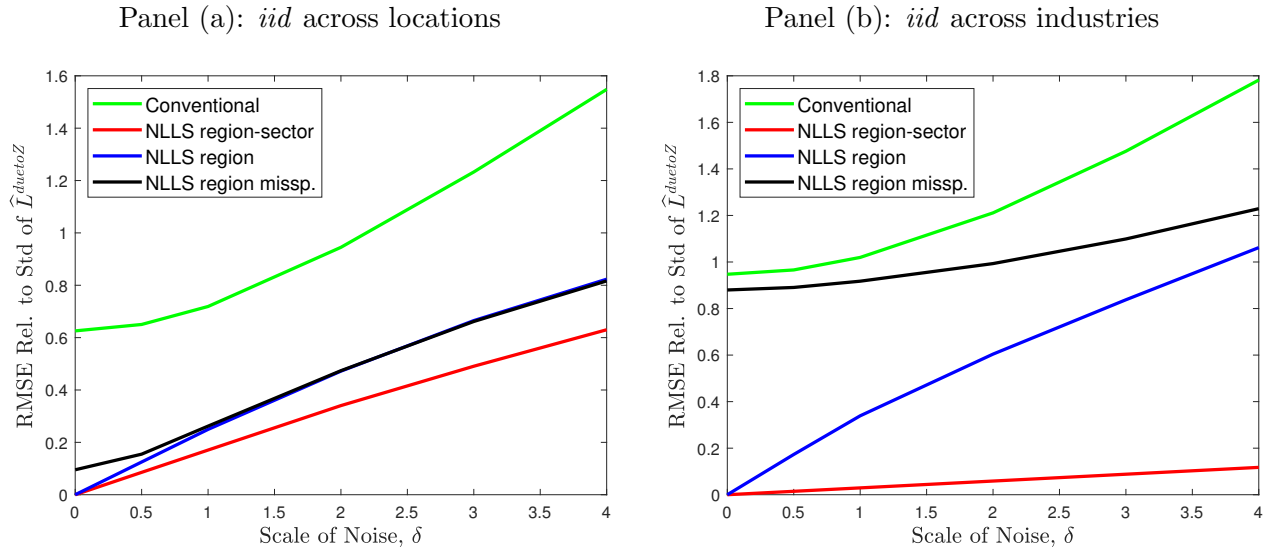
$$\mathbb{E} \left[\zeta_2' \left(\tilde{\Psi}^0\left(\frac{\theta}{\sigma}\right) - \tilde{\Psi}^0(\lambda) \right) (\hat{\mathbf{z}} - \mu\iota) \right] = 0$$

by the law of iterated expectations.

We now show that $\frac{\theta}{\sigma}$ uniquely minimizes (43). The second term in 43 does not depend on λ . The first term is zero when $\lambda = \frac{\theta}{\sigma}$ and positive whenever $\tilde{\Psi}^0(\lambda) \neq \tilde{\Psi}^0\left(\frac{\theta}{\sigma}\right)$ since the variance-covariance matrix of $\hat{\mathbf{z}}$ is non-degenerate. However, $\tilde{\Psi}^0(\lambda) = \tilde{\Psi}^0\left(\frac{\theta}{\sigma}\right)$ implies $\Psi^0(\lambda) = \Psi^0\left(\frac{\theta}{\sigma}\right)$ and in turn $\lambda(I - \Gamma^0\Pi^0) = \frac{\theta}{\sigma}(I - \Gamma^0\Pi^0)$, which is impossible for $\lambda \neq \frac{\theta}{\sigma}$ as long as there is any mobility in the steady state, i.e. $\Gamma^0\Pi^0 \neq I$.

Appendix Figures and Tables

Figure A1: Robustness of RMSE Measures to Noise Scaling



Notes: This figure repeats the analysis of Table 4 varying the noise scaling factor δ , which multiplies the error term ζ in the simulations. Panel (a) reports the root mean-squared error (RMSE) of the four methods relative to the RMSE of the uninformative prediction for *iid* location shocks, while Panel (b) uses *iid* industry shocks. See notes to Table 4 for details.